ON VISCOUS FLOW PARAMETERS

A: Martellucci H, Rie

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FOREWORD

This report presents the results of work performed by the General Electric Re-entry and Environmental Systems Division during the second half of CY 1970 under Contract F04701-70-C-0179 which is jointly supported by SAMSO and ARPA. The work was accomplished under Task 4.8 (Reentry Aerodynamic Technology) of the STREET G Program and was monitored by Capt. R. Padfield (U.S. Air Force, SAMSO) and R. Mcore (ARPA).

This report has been reviewed and is approved.

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ABSTRACT

Boundary layer measurements on a 7.25 degree cone at Mach 8 in a Reynolds number range of 0.65×10^6 to 3.7×10^6 per foot have been analyzed and correlated. Boundary layer displacement and momentum thicknesses computed from the measured data are compared with values given by currently used empirical correlations for turbulent as well as laminar flows. An improvement to the correlations for boundary layer thicknesses in turbulent flows at zero mass addition rate is proposed. A new set of equations expressing the dependence of turbulent boundary layer thicknesses on mass addition rate is also proposed. The changes are shown to result in improved agreement between empirical predictions and flight data as well as ground test data.

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LIST OF SYMBOLS

| LIST OF SY | MBOLD |
|---------------------------------------|---|
| A | area |
| A _b | model base area |
| c | Chapman-Rubesin constant: $C = (\mu * T_e)/(\mu_e T^*)$ |
| CD | drag coefficient |
| c _f | skin friction coefficient |
| c _F | mean skin friction coefficient: $C_F \equiv \iint_{A_S} C_f dA/As$ |
| c _M | pitching moment coefficient |
| c_N | normal force coefficient |
| $D_{\mathbf{b}}$ | base diameter |
| h | enthalpy |
| Н | stagnation enthalpy, also form factor: $H \equiv \delta */\theta$ |
| L | model length |
| m° | mass addition rate |
| m | integrated mass addition rate: $\tilde{m} = (\iint (\rho_w)_w dA)/(\rho_w V_w A_b)$ |
| Й | Mach number |
| Mw | molecular weight |
| $\widetilde{\mathtt{M}}_{\mathtt{W}}$ | molecular weight ratio: $\widetilde{M}_{W} = (M_{W})_{b.1.} / (M_{W})_{inj.}$ |
| MF | Mangler factor |
| n | power law velocity profile exponent |
| p | presure |
| P _o ' | pitot pressure |
| q | dynamic pressure, $\frac{1}{2} P V^2$ |
| ģ | heat transfer rate |
| r _b | radial coordinate to model surface (in cyclindrical coordinate system) |
| R _b | base radius |

```
Re
               Reynolds number
               Reynolds number based on wetted length
               model nose radius
R_{N}
               radial coordinate to bow shock wave (in cylindrical
Rg
                   coordinate system)
               wetted length
               Temperature
               u/ue
               velocity components parallel and normal to model surface
                velocity magnitude
                   \gamma_{\rm inj}/\gamma_{\rm b.l.}
                axial distance from cone vertex
                normal distance from model surface
                angle of attack
                boundary layer thickness
                displacement thickness
Δx<sub>tr</sub>
                distance downstream of end of transition
                ratio of specific heats
                exponent used with profiles in Crocco coordinates (eqn. 18)
                mass addition parameter: \zeta = 2 \lambda / C_{f_0}
 0 >
                momentum thickness
\theta_{b}
                model surface inclination from axial
                value of \theta_b on conic portion of model
                mass addition parameter: \lambda = (P v)_w / (P u)_{e_0}
 H L
                dynamic viscosity
```

kinematic viscosity density meridional angle SUBSCRIFTS model base b b.1. boundary layer conic value boundary layer edge initial value i inj. injectant local value model length L mean value pressure contribution recovery condition model surface stagnation condition at transition tr model wall at zero mass addition rate 0 free stream (upstream of bow shock)

Eckert reference condition

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SECTION I

INTRODUCTION

Despite the considerable analytic and experimental work on compressible turbulent boundary layers which has been performed in recent years, a satisfactory and general description is still lacking. The basic complexity of turbulent flow has led those seeking to describe the compressible case to hypothesize similarities between the compressible boundary layer and the constant density boundary layer, where at least a larger body of experimental measurements is available.

No attempt will be made here to review the numerous analytic investigations of compressible turbulent flow which have been made in recent years; however, mention of some recent references for background is in order. The work by Spalding and $\mathrm{Chi}^{(1)}$ included a rather comprehensive review of current theoretical methods as well as a semi-empirical theory. The transformation approach developed by $\mathrm{Coles}^{(2)}$ has been modified by $\mathrm{Crocco}^{(3)}$ and extended and applied by Baronti and Libby $\mathrm{Libby}^{(4)}$. Economos $\mathrm{Libby}^{(5)}$ recently developed a phenomenological treatment for solving the compressible turbulent boundary layer with mass addition which is a generalization of the work of Baronti and Libby $\mathrm{Libby}^{(4)}$.

Another approach to this complex problem is to adapt methods which have proven successful in solving the laminar boundary layer. In this approach, investigators have used an eddy viscosity concept to express the Reynolds stress terms which occur in equations governing turbulent boundary layer flow. The result is a set of equations for the turbulent boundary layer which differ from the equations governing laminar boundary layer flow solely in that molecular viscosity and Prandtl number are replaced by an "effective" viscosity and Prandtl number. If one can determine empirically what values to assign the effective viscosity and Prandtl number, it becomes possible to solve the mean characteristics of the turbulent boundary layer using well established methods for the solution of the laminar boundary layer. Eddy viscosity models for wall boundary layers have been developed by Kleinstein (6), Smith and Cebeci (7), Patankar and Spalding (8), and Sontowski (9) to name some of the more recent contributors. Each of these models was developed for the zero pressure gradient, zero mass injection case. All were shown by Martellucci, Rie, and Sontowski (10) to present reasonable agreement with data even when moderate rates of mass injection were considered. Cebeci, Smith, and Mosinkis (11) recently modified the viscosity model of Ref. 7 to include the effect of pressure gradient.

Attempts to compare the theoretical work with compressible turbulent flow experiments have been limited not only by the paucity of detailed data but also by the incomplete experimental definition of the mean profiles across the boundary layer in high speed compressible flow. This is especially true for the hypersonic case and where mass injection and other effects such as temperature jumps, which cause non similar profiles, are present.

And the content of th

Because of the complexity of the more rigorous analytic formulations, the numerical difficulties encountered in the solution of ablating vehicle boundary layers (due to the ablation rates, discontinuities, etc.), and the excessive computer times required to generate a solution, vehicle designers are forced to use engineering analyses which are formulated to solve the boundary layer equations. Due to the uncertainties introduced by these empirical relations, a high degree of rigor in the mathematical solution of the equation is not warranted. As a consequence, for the analysis of a turbulent boundary layer with mass injection, most authors(12-16) have utilized additional assumptions which have greatly simplified the mathematical solution of the equations. However agreement between existing theory and experimental data for a wide range of conditions is $poor^{(17-19)}$. A need exists for an analysis that minimizes the dependency on the assumptions usually employed to simplify the solution of the equations, but which retains the essence of the more rigorous formulations. These engineering analyses were generated by the various aerospace companies (20-25) for the prime purpose of computing the vehicle loads and drag (which implies an accurate definition of the local properties). Since these empirical analyses were formulated, additional data have become available which can be used to validate and/or update some of the empiricism that is inherent in these methods.

The objective of the current effort is to re-evaluate the influential mechanisms of interaction between re-entry body heat shield ablation and aerodynamic parameters, based upon data obtained under the preceding STREET-G contract, other ground test data, with analytic results, and with applicable flight test data. The specific objectives of this research are to improve (1) the empirical correlations which account for mass injection effects on the viscous layer thicknesses, (2) the basic turbulent relations for predicting the viscous properties, and (3) the validity of the Crocco integral for turbulent flows with mass injection. The influence of the improved correlations on the vehicle drag for some typical flight vehicles is also ascertained.

SECTION II

EXPERIMENT DESCRIPTION

Since the primary data that are to be used in the current research were obtained and reported under the preceding STREET-G program (26), only a brief description of the test facility, the test model, and the boundary layer probes is in order.

2.1 TEST FACILITY

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The test program was conducted in the Arnol? Engineering Development Center (AEDC) Tunnel B at Mach 8. This facility is a continuous flow, hypersonic wind tunnel with a 50-inch diameter test section. Interchangeable axisymmetric contoured nozzles provide flow at either Mach 6 or 8. The tunnel is a closed circuit type which operates over a range of pressures with air supplied by a central compressor system. A model injection system provides the capability for quick model changes without interrupting tunnel operation. The tunnel flow conditions provide free stream Reynolds numbers from 0.30 x 10^6 to 3.3 x 10^6 per foot at Mach 8 with a maximum total temperature of 1350° R. A sketch of the tunnel layout and a summary chart of the performance characteristics of the facility are shown in Figure 1.

Model support and sting assemblies provide a 30-degree pitch range capability. A number of conventional internal strain gage balances is available at the facility to measure data in many ranges of forces and moments, and proper balance selections may be made for accuracy at small angles of attack or for a range to cover the larger angles of attack. Model support in the tunnel is positioned so that dual windows can provide complete flow visualization and photography. Each window is equipped with either a conventional single pass Schlieren system or a parallel beam refocused shadowgraph system. Model attitude in the tunnel was measured by the data readout system and verified optically with a scope in both the pitch and yaw planes. The angle of attack was maintained to within + 0.10 for this entire investigation.

2.2 TEST_MODEL

The model used in this investigations was a 7.25° half angle cone with a tangent full dome afterbody. The cone base diameter is 10.6 inches. A sketch of the model is presented in Figure 2. Three thermocouples are installed in the model one in each porous chamber. Additional pressure taps are located inside the model for use in calibration prior to the test.

The model is longitudinally divided into four separate sections. The nose section is fabricated from stainless steel. Sections one and two are fabricated from a porous sintered nickel-stainless steel alloy which is approximately 60 percent dense. The rear plate of the last conical section is adapted to accommodate the hollow compression-strut support system used for the pressure measurement phase. The last section is the impervious

tangent aft-dome. It is made of stainless steel and was spin formed. This section has cutouts in it to accommodate the legs of the strut support system. A second dome section had a hole in the center to accommodate the sting mount system, which was used for force measurements.

The internal structure of the model is fabricated to house the balance water jacket and sting arrangement to be used during the force measurement phase. The internal plusbing of the model is designed to exhaust gas into a common plenum at the rear of the model inside the last section. The gas is dispersed forward through sonic orifices into the two porous sections of the model. The mass addition rate is controlled by the plenum pressure and the distribution of the mass addition is controlled by the relative areas of the sonic orifices to the individual chambers.

The blowing or porosity uniformity of the model was established prior to the test with a venturi calibrating device. The calibration was performed with the external surface of the model at atmospheric conditions. It was performed with a conical venturi which had a twenty to one contraction ratio with a throat area of 0.05 square inches. The differential pressures between throat and plenum were recorded with a \pm 1 PSID transducer. The gas samples were obtained by attaching a contoured rubber adaptor which was fitted to the cone surface. The capture area of the adaptor was roughly 0.5 square inches. The venturi was calibrated with the AEDC facilty reference sonic orifices. Localized mass flux readings, $(\rho v)_w$, were obtained along several rays of the model which were 45 degrees apart. The calibration indicated that the model porosity was symmetric to within \pm 25%. A sample of the calibration data is given in Figure 3.

2.3 BOUNDARY LAYER PROBE

A pitot pressure and a total temperature probe were used to determine the details of the boundary layer during the course of this investigation. The probing apparatus was designed to present both probes to the flow with a separation distance of approximately 1/2 inch. The probing was performed with each probe 1/4 inch off of the vertical meridian of the model at all angles of attack. This offset was accounted for in the data tabulations and plots. The probes and their supporting structure were included 7.25 degrees to the centerline to minimize interference with the flow over the cone. The temperature probe was a singly shielded thermocouple with a diameter of 0.060 inch. The total head probe was a .040 inch diameter hyperdermic tube.

SECTION III

EFFECT OF BLOWING RATE NON-UNIFORMITIES ON BOUNDARY LAYER PROPERTIES

Prior to discussing the analysis of the data obtained with the porous cone described in Section 2, some words are in order with regard to the sensitivity of experimental data to the nonuniformities in porosity which are indigeneous to each particular model.

Aerodynamic test models fabricated from porous materials have commonly been used to simulate ablation in wind tunnel experiments. These models have been constructed from a variety of porous materials that are currently available commercially. For impulse facilities, such as AEDC tunnel F (hotshot) LTV, and at GE, thin skinned models (.030" to .060") were generally fabricated (rolled and welded) from material supplied by Union Carbide, Keendan Associates, from the Pail Corporation. For the more severe heating loads and environment imposed on models tested in the continuous flow facilities at AEDC tunnels B and C, these thin skin models are unsuitable. In these facilities, models fabricated from a porous material with a thicker wall (~.25") are necessary. Materials such as the sintered metal of Mott Metallurgical Corporation or the Poametal material of GE Metallurgical Products Division are therefore required from a thermal stress viewpoint.

Regardless of the porous material selected, the porosity distribution - that is the blowing rate distribution over the model - must be known for each experimental investigation. For all the materials, the forming process in making the bulk material into a test model creates certain nonuniformities in the blowing rate. If a porous model is to be used to investigate the boundary layer details in a turbulent mixing investigation for example, one must ascertain what nonuniformities are tolerable from a data accuracy point of view.

The purpose of this section is to demonstrate with experimental data and also with a theoretical calculation conducted with the Equilibrium Nonsimilar Boundary Layer Program (ENSBL) (27), the insensitivity of the mean boundary layer properties to the deviations from the average blowing rate.

3.1 NUMERICAL VERIFICATION

The Equilibrium Non-Similar Boundary Layer Program (ENSBL) was used to investigate the effect of the distribution of mass addition rate on the character of the boundary layer. Calculations were carried out on a sharp 7.25 degree cone for Mach number 8. It is evident (Figure 3) that the blowing distribution for this model is not constant but varies some \pm 50% about the mean value, with \pm 25% variations in axisymmetry.

Numerical results were computed for both the uniform and the nonuniform (sawtooth) axisymmetric blowing distributions shown in Figure 4. In one case, a uniform mass addition rate was applied over the posous portion of the cone $(9.19 \le \text{X/L} \le 0.90)$. Outside of this range the mass addition rate was zero.

In a second case, the "sawtooth" distribution of mass addition rate was used. This distribution corresponds to a fairing of the data of Figure 3. Total mass added was the same in the two cases. Representative results are plotted in Figures 4 through 6.

Qualitatively, the displacement thickness responds as expected to the mass addition rate. Initially (0.66 \leq X \leq 1.18 ft.) the mass addition rate is greater in the uniform \hat{m} case, as is the displacement thickness. For 1.18 ft. \leq X \leq 2.24 ft. the sawtooth \hat{m} exceeds the uniform value, and $\hat{0}^*$ for the sawtooth case grows faster than for the uniform case. At X \approx 2.59 ft and X > 3.14 ft. the mass added to the boundary layer forward of that station is the same in the two cases, as is the value of displacement thickness.

Quantitatively, the response of the δ^* curves is less than proportional to the variations in mass addition. At X \approx 1.9 ft., where the mass addition rate for the sawtooth case is 53% greater than that of the uniform case, the difference in displacement thickness is only 6%. At X = 2.2, where mass added to the boundary layer in the sawtooth case is 15% greater, the difference in δ^* is only 8%.

Figures 5 and 6 present velocity and stagnation temperature profiles at X = 2.2 ft. (where the maximum difference in mass added occurs) and at X = 3.065 ft. (where total mass added in the two cases is the same). As might be expected, the difference between the two cases is greater in Figure 5. However, the differences between the two cases is insignificant*. The maximum difference in temperature profiles is less than 1%, whereas the maximum difference in velocity profiles is less than 2%.

The conclusions which can be drawn from this comparison are: because of the increased mixing characteristics in a turbulent boundary layer, a difference in the mass addition rate distribution about a mean value does not appear to significantly affect the character of the boundary layer; and that the boundary layer depends primarily on average mass addition rate, and appears to be relatively insensitive to fluctuations in the upstream history of the mass injection.

3.2 EXPERIMENTAL VERIFICATION

Force and moment data were obtained with the porous model mounted on a strain gage balance. Data were obtained for several blowing rates. If the blowing nonuniformities cause an asymmetric configuration to result, then a residual moment and normal force would appear at $\alpha=0^{\circ}$. However, data obtained with this model, as shown in Figure 7, show no such influence.

It can be concluded that useful and meaningful experiments can be conducted to investigate the turbulent boundary layer characteristics of an ablating cone, simulated by blowing, with a model which exhibits blowing nonuniformities of ± 50% about the mean.

It should be noted that a highly expanded temperature scale was used, i.e., only the range $0.8 \le T_0/T_0 \le 1.0$ is shown.

SECTION IV

ANALYSIS AND CORRELATION OF TURBULENT BOUNDARY LAYER DATA

The experimental results obtained from the boundary layer profile measurements, which include the effects of mass injection, are presented and discussed in the following sections. The data analyzed are for both turbulent and laminar boundary layer flows, although emphasis is placed on the turbulent data. For the turbulent data, the effect of mass injection on such properties as the boundary layer thickness, displacement and momentum thicknesses, velocity profile exponent and the applicability of the Crocco theory are discussed. The data analyzed are presented in graphical form in the body of the report; tabulations of the profile properties deduced from the measured data are contained in the Appendix A. Also included in this report are the free stream and local properties (i.e. wall temperature, pressure, transition location, etc.) that are associated with the profile measurements.

4.1 DATA ANALYSIS AND PRESENTATION

The boundary layer profile data that were obtained with the porous cone shown in Fig. 2 for both the 1969 STREET-G program(26) and also for the 1968 Mark 12 Penetration Aids program(28) will be presented in this section. For convenience and clarity of presentation, the data were coded to denote the free stream environment, blowing rate and distribution, the injectant, and the state of the boundary layer at the profile measurement station. Each case is assigned a letter index which denotes the free stream condition, the average blowing rate and distribution, and the state of the boundary layer at the measured profile station (see Table I). A single letter denotes the data acquired on the 1969 STREET G Program(26). A double letter denotes data acquired on the 1968 Mark 12 P/A effort(28); moreover, the second letter L denotes laminar data. Each case is assigned a data symbol which will be used consistently throughout the report (see Table I). For each case surface pressure, force data, and boundary layer profile data at several stations were obtained from Reference 26. The AEDC data group numbers corresponding to each case may be found in Table 2. Average free stream test conditions for each case may be found in Table 3.

4.1.1 WALL TEMPERATURE DISTRIBUTION

The model wall temperature distributions were determined for each blowing condition, at each Reynolds number. The temperature distributions as determined from the three thermocouples located in the porous sections are shown in Figure 8. These values correspond to the equilibrium wall temperature that is achieved prior to and maintained during the acquisition of the profile data. For each Reynolds number, the wall temperature as deduced from each thermocouple correlates with the local average blowing rate, and as shown in Figure 8 is reduced as the blowing rate increases. This was also true for the non-uniform blowing cases (M and N).

4.1.2 TRANSITION ZONE DEFINITION

Measurements to deduce the state of the boundary layer were not made during the 1969 STREET-G tests, primarily because these measurements were available from the prior test entry (28). The state of the boundary layer was determined from the impact pressures measured by traversing a pitot probe along the model surface. Data to assess the effect of mass addition on boundary layer transition were obtained for one test condition (i.e. Re_{\bullet} /ft = 2.7 x 10^{6}) and are shown in Figure 9. Variation of onset and end of transition with mass addition rate were deduced from Figure 9, and are plotted (solid lines) in Figure 10. The location of the transition zone for the second test condition (i.e. Re_{∞}/Ft . = 3.7 x 10°) was obtained for the non blowing case only. The m effects at the higher Reynolds number condition (dotted lines) were then scaled from the data available at the lowe: Daynolds number. It is apparent from the dip (near \dot{m} = .01) in the data shown in Figure 10, that a slight transition reversal occurred. The initial forward movement can be attributed to the destabilizing influence of mass addition on transition. However, as the blowing rate increases, the wall temperature decreases. In this temperature range, the latter effect is stabilizing, and apparently is dominant, so that as the blowing rate increases beyond 0.01 transition moves aft. Furthermore, the data indicate that the local wetted length Reynolds number (Res) at the end of transition is roughly 8-9 x 10^6 . In a later discussion concerning the data of Danberg (29) the above information will be used to indicate that some of the data presented therein are not turbulent but are transitional.

4.1.3 MASS ADDITION RATE DISTRIBUTION

Consistent with the calibrations performed with the porous model at AEDC, the mass addition rate distributions were scaled to conform with the basic colibration and the integrated (metered) mass rate to the model. Listed in Table 4 are the mass addition rate schedules for Cases A through N.

4.1.4 BOUNDARY LAYER PROFILE MEASUREMENTS

As indicated in Section 2.3, boundary layer profile measurements (i.e. pitot pressure and total temperature) were made at several axial stations (see Figure 2). The Rayleigh formula (30) was used to compute the Mach number from the measured pitot pressure and the static pressure which was assumed constant in the boundary layer and equal to the wall static pressure. The wall static pressure was measured by crifices in the model surface in the absence of the profile probes. The velocity in the boundary layer was computed from the local value of the Mach number and the measured total temperature. Using adiabatic relations (30) in this manner boundary layer properties such as density, temperature, and velocity which are required to compute the displacement and momentum thicknesses were defined. The displacement and momentum thicknesses were determined from the following relations:

$$\delta * = -\frac{r_b}{\cos \theta_b} + \left[\left(\frac{r_b}{\cos \theta_b} \right)^2 + 2 \qquad \int_0^{\delta} - \left(\frac{r_b}{\cos \theta_b} + y \right) \left(1 - \frac{\rho_u}{\rho_e u_e} \right) dy \right]^{-1/2}$$
(1)

$$\theta = -\frac{r_b}{\cos \theta_b} + \left[\left(\frac{r_b}{\cos \theta_b} \right)^2 + 2 \int_0^{\delta} \left(\frac{r_b}{\cos \theta_b} + y \right) \frac{\rho_u}{\rho_e u_e} \left(1 - \frac{u}{u_e} \right) dy \right]^{1/2}$$
 (2)

Inherent in the above relations are the corrections which account for transverse curvature. The boundary layer thickness was established consistently from the total temperature profile, which for the sharp cone also agrees with that obtained from the pitot pressure profile. Tabulations of the local conditions and profile parameters may be found in Appendix A. For Re_{∞} /ft = 3.7 x10 6 (cases A through E) the axial distribution of δ , δ , and θ may be found in Figures 11 through 13, and for Re_{∞}/ft = 2.7 x 10 6 (cases F through J) in Figures 14 through 16. The increase in the viscous thickness due to mass injection is rather evident from these figures. It will be shown that mass transfer increases each thickness roughly linearly with the blowing parameter $\frac{(\rho_{\nu})}{(\rho_{\nu})}$. Also shown in these figures is the boundary layer $\frac{2}{(\rho_{\nu})} \frac{(\rho_{\nu})}{(\rho_{\nu})} \frac{(\rho_{\nu})}{(\rho_{\nu$

transition zone: for $\dot{m}=0$. As noted, the forward profile station (X/L = 0.35) is in the transition zone. Also shown on these figures is the zero mass addition, all turbulent boundary layer prediction of Walker(31), as computed by VIZAAD(20). For the sharp cone, Walker's relations are simply defined as

$$\theta = 0.037 \text{ (MF)} \quad \frac{(\rho_*)^{0.8}}{\rho_e} \quad \left(\frac{\mu^*}{u_e}\right)^{0.2} \quad s^{0.8}$$
 (3)

where MF is the Mangler factor

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$$\frac{\delta}{\theta} = 8 + \left(1.29 \frac{h_{\rm w}}{h_{\rm r}} + 1\right) \left(1 + 3.02 \sqrt{\frac{H_{\rm e}}{h_{\rm e}} - 1}\right) \tag{4}$$

$$\frac{\delta^*}{\theta} = -1 + \left(1.29 \frac{h_{\rm w}}{h_{\rm r}} + 1\right) \left(1 + 2.08 \sqrt{\frac{H_{\rm e}}{h_{\rm e}}} - 1\right)$$
 (3)

where equations 4 and 5 are valid for Me ≥ 4.5. It is evident that modifications must be made to these simple engineering relations for the zero mass addition case in order to account for the influence of mass injection. This will be discussed in Section 5.1.

Turbulent boundary layer velocity profiles are cystomarily characterized by the power-law relation

$$\frac{u}{u_e} = \left(\frac{Y}{\delta}\right)^{\frac{1}{n}} \tag{6}$$

The exponent, n, was obtained by measuring the slope of the velocity profile plotted on log-log paper. The axial distribution of n for Cases A to E is shown in Figure 17, and for Cases F through J in Figure 18. For the zero injection case at ${\rm Re}_{\infty}$ /ft = 3.7 x 10^6 , the axial distribution is characterized by a value of n ≈ 9 at the forward transitional station, an increase to some unknown value (n $\gtrsim 12$) at the end of transition, then by a decrease to values of the order of 7 at points sufficiently far removed from the end of transition. This is in concert with the study performed by Johnson and Bushnell $^{(32)}$ wherein a data summary concerning the power law sensitivity to Reynolds number. Mach number, and wall cooling was made (Figure 19). The Johnson-Bushnell $^{(32)}$ data survey indicated that the velocity exponent actually experiences an overshoot beyond the classical turbulent value of n \approx 7 at points immediately downstream of transition. It was postulated that n correlates with the incremental distance downstream of the end of transition normalized by the boundary layer thickness (Δ X_{tr}/ δ). However, the present data do not appear to support this hypothesis. Nonetheless, values of the velocity exponent in excess of seven were experienced in the region immediately downstream of transition.

The effect of mass transfer on the turbulent velocity profile shape is to make it less full and as a result the exponent n is reduced as shown in Figures 17 and 18. A decrease of n to some 30% of its no blowing value is noted for a blowing rate $\zeta = 9$.

4.2 DATA CORRELATIONS AND COMPARISONS

To assess the influence of mass addition on the viscous layer thicknesses, the turbulent data available in Refs. 26 and 28 were presented in a form where the normalized thickness ratio (blowing value to the no blowing value) were plotted against the blowing parameter, ζ . The values of Cf₀ and (θ u) eo represent local properties at the profile station for the non-blowing case. The thickness growth with blowing for δ/δ_0 , $\delta*/\delta*$ and θ/θ are shown

in Figs. 20 to 22, respectively. Also included in these figures are the turbulent flat plate data of Danberg (29) where the ζ value was corrected by the Mangler factor. Good agreement and correlation is noted for all the data. As mentioned earlier, the data presented by Danberg correspond to data obtained for two separate ranges of wetted length Reynolds number, $R_{\rm es}$; one covering the range $R_{\rm es}$ of 3 x 10° to 6 x 10°, and the second covering the range 8.5 x 10° to 11 x 10°. It is postulated, that based upon the available boundary layer transition results, that the data obtained for the lower Reynolds number range correspond to transitional boundary layer data. When these data are included in the correlation, although agreement is achieved with the mean levels of the "turbulent" data, considerably more scatter is evident. Consequently, in the correlations shown in Figs. 20 to 22 only data for $R_{\rm es} \ge 9 \times 10^6$ are included. Best fit curves were established for each of the ratio's in the form of simple algebraic relations. That is:

$$\delta/\delta_{0} = 1 + 0.262 \,\zeta - 0.00627 \,\zeta^{2} \tag{7}$$

$$\delta * / \delta * = 1 + 0.333 \zeta$$
 (8)

$$\theta/\theta_{0} = 1 + 0.410 \zeta \tag{9}$$

As a result of these curve fits, the effect of mass addition on the form factor H \odot $\delta*/\theta$ becomes

$$\frac{H}{H_0} = \frac{1 + 0.333 \,\zeta}{1 + 0.410 \,\zeta} \tag{10}$$

A comparison of this relation and the data is shown in Fig. 23. It is evident from these data that mass addition tends to lower the form factor so that at $\zeta \approx 9$, there is roughly a 15% reduction. This is in contrast to all of the existing turbulent correlations (20,21,22) which assume that blowing has no effect on the form factor (i.e. $H = H_0$).

Also shown in Figs. 20 to 22 are the curves corresponding to the current empirical prediction techniques of General Electric $^{(20)}$ McDonnell Douglas $^{(22)}$, and Philco Ford $^{(21)}$. The analytic form for each of these relations is expressed below:

General Electric (20)

$$\delta/\delta_{0} = \frac{1}{2} \quad \left[\frac{4+\zeta}{2+\zeta} \right] \quad \frac{\theta}{6} \tag{11}$$

$$\delta */\delta_{0}^{*} = \theta/\theta_{0} = 1 + 0.752 \,\zeta + 0.0189 \,\zeta^{2} \qquad (0 \le \zeta \le 6.55) \quad (12)$$

$$\delta */\delta_{0}^{*} = \theta/\theta_{0} = 0.185 + \zeta \qquad (\zeta > 6.55)$$

McDonnell Douglas (22)

$$\delta/\delta_{o} = \frac{1}{1 + 0.143 \zeta} \left(\frac{\theta}{\theta_{o}}\right) \tag{13}$$

$$\delta^*/\delta^*_0 = \theta/\theta_0 = \frac{W^{0.8} \zeta}{(1+W^{0.8} \zeta/4)^4 - 1}$$
 (14)

where W = $\gamma_{inj}/\gamma_{b.l.}$

and y is the ratio of specific heats

Philco Ford (34)

$$\delta^*/\delta_o^* = \theta/\theta_o = \left(\frac{T^*}{T_o^*}\right)^{-0.6} \left(\frac{C}{C_o}\right)^{0.2} \left(\zeta + \frac{C_f}{C_{f_o}}\right)$$
(15)

$$\frac{C_{f}}{C_{f_{0}}} = 1 + \frac{1}{2} \left(\widetilde{M}_{w}^{0.46} \widetilde{u} \zeta \right)^{2} - \frac{1}{2} \left(\widetilde{M}_{w}^{0.46} \widetilde{u} \zeta \right) \left[\left(\widetilde{M}_{w}^{0.46} \widetilde{u} \zeta \right)^{2} + 4 \right]^{1/2}$$

where
$$c = \frac{\mu^*}{u_e} = \frac{T_e}{T^*}$$
 (Chapman-Rubesin Const.)
$$\widetilde{M}_{w} = \frac{(M_{w})_{b.l.}}{(M_{w})_{inj}}$$
(Mw = molecular weight)

and
$$\widetilde{u} = \frac{u_L}{u_e} = 10.5 \quad \left[\frac{T_w}{T_e} \frac{C_{f_0}}{2} \right]^{1/2}$$
 (17)

It is evident from the data comparisons that each of the techniques described above overpredicts the effect of mass addition on the viscous layer thicknesses.

The effect of mass addition on the velocity profile exponent is shown in Fig. 24. It can be seen from this figure that a considerable distortion of the velocity profile results from mass addition. Furthermore, the scatter of the results suggests that parameters in addition to ζ are necessary to better correlate the data.

4.2.1 SENSITIVITY OF RESULTS TO ANGLE OF ATTACK

It is desirable to assess the sensitivity of the data used in the correlations to various sources of error, for example to the model angle of attack. This is particularly true of the results presented in Figures 20 through 24, since experimental error is magnified in obtaining ratios of two measured quantities. Although deliberate care was taken to align the model precisely with respect to the encoming stream (i.e. $\Delta \alpha = \pm 0.1^{\circ}$) some misalignment is always present. Boundary layer profiles were obtained on the windward and leeward rays of the model at selected stations for $\alpha = \pm 1$ (see Ref. 26). A data reduction procedure similar to that used for the $\alpha = 0^{\circ}$ cases was used with the $\alpha = \pm 1^{\circ}$ zero mass addition data at x = 41.51 inches (that is, cross flow effects were neglected). Shown in Fig. 25 are the results of this calculation. An error of $\pm 2\%$ in thickness would result for a $\pm 0.1^{\circ}$ angle of attack. However the effect of angle of attack on the velocity profile exponent is negligible, to within the accuracy of the data. Consequently the data scatter, evident in Figure 24, must be attributed to other causes.

4.2.2 COMPARISONS OF DATA WITH THE CROCCO RELATION

Theoretical and semi-empirical approaches to the solution of a turbulent boundary layer rely upon several approximations, one of which is the Crocco relation for unit Prandtl number, $\frac{H-h}{H_e-h_u} = u/u_e.$ The bulk of available

experimental data indicate that only for the adiabatic wall case does the

unit-Prandtl number Crocco relation agree with the data. In terms of the total enthalpy profile, the summary of experimental results reported by Bertram and Neal (33) indicates consistently lower values of total enthalpy in the turbulent boundary layer than the Crocco relation (see Fig. 26). Purely as an empiricism, a curve for $\frac{H-h}{H_e-h} = \left(\frac{u}{u}\right)^2$ also drawn in

Fig. 26, and is seen to describe much more adequately the experimental results than the classical linear Crocco relation. Included in this figure are the results of the present investigation (26). For the present data, the absence of data at $u/u_e < .7$ is due to the difficulty of obtaining accurate measurements in the relatively thin boundary layers present on slender cones in hypersonic flows. Nonetheless, the present data for the non-blowing case agree with the data summary of Bertram and Neal (33).

The effect of blowing on the total enthalpy profile for all stations in case E may be seen in Fig. 27. In this case, due to the boundary layer thickening resulting from mass addition, data were obtained down to $u/u_e = 0.27$. Furthermore, the accuracy of the measurement (reduction of scatter) is also shown to increase. It is evident from this figure that for a given value of u/u_e mass injection tends to increase the total enthalpy in the boundary layer over the zero \dot{m} value. A consistent trend was noted for all of the data obtained, wherein, an increase in blowing affected the level of the total enthalpy in the boundary layer (Fig. 28). Thus, if one represents the enthalpy profile by the relation

$$\frac{H - h_{w}}{H_{e} - h_{w}} = \left(\frac{u}{u_{e}}\right)$$
 (18)

the value of ϵ (shown in Fig. 29) tends to decay with increased mass addition. It was tacitly assumed that ϵ = 2 best represents the zero mass addition data.

4.3 DATA COMPARISONS WITH THEORY

Comparisons of the boundary layer thickness data with the General Electric Theories, such as the Viscous Interaction Zero Angle of Attack Drag (VIZAAD), and the Equilibrium Non Similar Boundary Layer (ENSBL) Programs, will be made in this section. The techniques employed in the current versions of each of these programs (10, 27, 20) are nominally equivalent to those employed industry wide and, consequently, the comparisons serve to show where deficiencies in the current state of the art exist. In addition, the implication of the recommended changes to the VIZAAD program on flight data predictions will be assessed.

4.3.1 COMPARISONS OF DATA WITH VIZAAD PROGRAM

Predictions of the viscous layer thickness as generated by the VIZAAD program were compared with data cases A through E as shown in Figs. 30 to 34.

In these VIZAAD computations, the flow was treated as laminar up to the point of transition onset. Downstream of this point, the flow was treated as turbulent. The effective origin of the turbulent solution was established by matching the zero blowing laminar momentum thickness to the zero blowing turbulent momentum thickness, that is (θ) LAMINAR = (θ) TURBULENT. As a consequence the values of the boundary layer thickness, δ , and the displacement thickness, δ^* are discontinuous at the transition point even for the zero mass addition case. For the cases with mass injection, all three thicknesses suffer the discontinuity since the thickness correlations differ at this point. For the cases under consideration, transition onset was sufficiently far forward so that the influence of this discontinuity on the downstream values is small. It is evident from Figure 30 that the original correlations grossly underpredict the viscous layer thicknesses. Implicit in the constant of equation 3 for computing the momentum thickness, is the assumption that the velocity profile exponent θ in the entire turbulent regime is 7. For a flat plate, the origin of θ stant may be found in Schlichting θ which can be summarized as follows:

For the general case of the power law $u/u_e = (y/\delta)^{1/n}$ we have

$$\frac{\theta}{\delta} = \frac{n}{(1+n)(2+n)} \tag{19}$$

and

$$\delta = 0.0575 \left(\frac{\nu}{u_{\infty}}\right)^{0.2} \left[\int_{0}^{x} \frac{(1+n)(2+n)}{n} dx\right]^{0.8}$$
 (20)

which for n = 7 becomes:

$$\delta = 0.37 \times \left(\frac{u_{\infty} \times v}{v}\right)^{-0.2}$$
 (21)

and

$$\theta = 0.036 \times \left(\frac{u_{\infty} \times v}{v}\right)^{-0.2}$$
 (22)

However, the experimental value of n is larger than the theoretical value predicted by Equation 3. This implies that n should be greater than 7, which is what the values deduced from the profiles indicate. If a functional relation n (x) were known, the constant could be revised accordingly, through the use of equation 20. However, this is not generally known. From the data of Cases A and F (that is for $\dot{m}=0$) one can deduce that the constant in the momentum thickness relation should be increased from 0.037 to 0.059. The displacement and the boundary layer thickness will increase proportionately as is evident from equations 4 and 5. The revised relations show good agreement with the data as seen in Fig. 30.

Since the effects of mass addition on the thickness are currently being overpredicted, the existing program tends to over compensate for the poor agreement at the lower blowing rates as is evidenced by Figs. 31 to 34. The relations defining the effects of mass addition in the program (that is equations 11 and 12) were replaced by the modified relations (equations 7 through 9). Shown in Figs. 31 to 34 are comparisons of the revised program with the data. It is noted in all cases, that good agreement was achieved by all three thicknesses.

For blunt bodies, the propercies at the edge of the boundary layer are determined (in VIZAAD) from the mass balance relation

$$\dot{m}_{\infty} = \dot{m}_{inj.} + \dot{m}_{b.l.}$$

or

and described the second of the contraction of the contraction of the second of the se

$$(\rho u)_{\infty} \pi R_{s}^{2} = \iint_{A_{s}} (\rho v)_{w} dA + 2\pi r_{b} (\rho u)_{e} (\delta - \delta^{*})$$
 (23)

It is evident that gross modifications to the thickness values will affect this balance and accordingly will affect the local properties and consequently vehicle drag. Flight data comparisons for two classes of slender vehicles were made and some of the results are summarized below. Vehicle 1, is a small-mass-loss ablator (i.e. has a high temperature heat shield), Vehicle 2, is a large-mass-loss ablator (i.e. has a low temperature heat shield). The initial bluntness ratio for both these vehicles is $R_{N_i}/R_B = .04$.

Comparison of Revised Program with Flight Data

| Vehicle No. | Altitude Kft | Vehicle Station | Parameter | Original Version of VIZAAD | Revised Version of VIZAAD | Flight Data |
|--|-----------------|--------------------|--|---|---|--|
| l High TempAblator m = .001 | 25 | X = .5L | δ (ft) δ* (ft) Me Res x 10-6 q btu/ft ² sec | .0264 .00813 3.50 12.66 273.9 | .0288 .00958 3.97 16.57 283.2 | |
| | | X = L | ô (ft) ô* (ft) Me Reg x 10 ⁻⁶ q Btu/ft ² sec | .0169 .00746 5.67 124.5 373. | .0223 .0101 6.73 210.6 382.7 | S. Carlos |
| | | | Total Vehicle Drag | .07 24 | .0743 | .082 |
| 2 Low Temp. Ablator $\tilde{m} = .049$ | 80 | X = .5L | δ (ft) δ *(ft) Me Res x 10-6 q Btu/ft ² | .0124 .00753 13.78 17.7 598 | .0164 .00857 14.30 20.2 579 | |
| | | X = L | δ (ft) δ* (ft) Me Re _s x 10 ⁻⁶ Å Btu/ft ² sec | .0431 .0320 14.5 41.5 | .0487 .0287 14.14 38.1 189 | |
| | | | Total Vehicle Drag | .0600 | .0570 | .043 |

For these comparisons the local boundary layer edge properties such as the Mach number and Reynolds number show significant variations where the bluntness effects are felt. Furthermore, in all comparisons with flight data, the revised version of the program predicted drag values closer to the data irrespective of whether the predictions were lower than or higher than the flight values.

Independent of the drag comparisons, large changes in the viscous layer predictions result from the modification. It will be shown in the next section that the results of the revised VIZAAD program agree better with the more exact ENSBL program predictions.

In addition to, and more important than the effect of the thickness perturbation on local properties, is the effect this change has on plasma attenuation. Here, there is interest in transmitting at higher frequencies, which implies shorter wave lengths. These wave lengths are of the coder of the boundary layer thickness and, consequently, the thickness of the layer and the shape of the profile (i.e. the local value of n) have a group effect on the plasma behavior. Shown in Figure 35 is the S band plasma attenuation profile with altitude for a slightly blunted slender re-entry vehicle. Also shown on this figure, at altitude h, is the plasma attenuation as computed by the method of Ref. 35 for two values of the boundary layer thickness. One was deduced from Walker's original relations (31) and the second was computed from the relations as modified in this report. The profile shape was similar for the two computations. One will note that the computation is sensitive to the thickness of the boundary layer, and furthermore the comparison with data is better with the modified thickness relations.

4.3.2 COMPARISONS OF DATA WITH THE ENSEL PROGRAM

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Comparisons of the ENSBL program were made with the data of Case A $(\vec{n}=0)$ and Case C $(\vec{m}=.01)$. In the former comparison, three different eddy viscosity models were employed in a manner similar to that discussed in Reference 10. For the latter, comparisons of the theory with one eddy viscosity model were made with the measured thicknesses.

Shown in Fig. 36 are the results of the ENSBL calculation compared to the data of (lase A. The three eddy viscosity models employed are those proposed by Smith and Cebeci⁽⁷⁾, Patankar and Spalding⁽⁸⁾ and by Sontowski⁽⁹⁾. In general the agreement of all three calculations with the measured total and displacement thicknesses is reasonable. However, one will note that the momentum thickness is underpredicted by the program irrespective of the viscosity model used. Examination of the velocity profile prediction in the physical coordinates (Fig. 37), and in the Crocco coordinates (Fig. 38) indicates that the total enthalpy in the viscous layer is being overpredicted. Of the three viscosity models, that proposed by Sontowski (which employs the lowest value of turbulent Prandtl number) most closely resembles the data (Fig. 38). However, additional modifications are required to effect acceptable agreement. The implications are that alterations to the turbulent Prandtl number, among other things, are required.

Comparisons of the ENSBL program, using Sontowski's eddy viscosity model, were made with data representing a case with mass injection as shown in Fig. 39. Once again, reasonable agreement is noted for the total and displacement thickness distributions. However, the momentum thickness is underpredicted as in the zero mass injection case. One can speculate that although mass injection increases the enthalpy in the viscous layer, the theory predicts larger values than those determined in the experiment.

ANALYSIS AND CORRELATION OF LAMINAR BOUNDARY LAYER DATA

The turbulent data reported in references (26) and (28) were discussed in the preceding section. Nine cases in which the boundary layer flow remained laminar (see Table 1) are also reported in Reference (28). The purpose of the present section is to compare the laminar data obtained in these cases, with currently used empirical correlations.

5.1 DATA ANALYSIS AND PRESENTATION

The boundary layer data in the laminar cases were obtained and reduced by the same methods as described in Section 4.1 for the turbulent cases. Displacement and momentum thicknesses were computed using equations (1) and (2). For this laminar data, they, as well as boundary layer thickness , δ , are plotted versus axial position in Figures 40 through 42.

To show their dependence of mass addition rate, the ratios δ/δ_0 , δ^*/δ_0^* and θ/θ_0 are plotted vs ζ (Figures 3 through 45). Although cases QL and SL provided data for values of ζ near 30.0, too few points were available at these high mass addition rates to warrant presentation. Figures 40 through 45, were, therefore, limited to $\zeta \le 3.0$. As might be expected, the data show a general thickening of the boundary layer with an increase in mass addition rate.

5.2 DATA COMPARISONS WITH CURRENT THEORY

Laminar thickness predictions of Walker (38) as computed in VIZAAD (20) are compared with experimental values in Figures 40 through 42. Walker's relations for laminar flow are:

$$\delta = \frac{5.3 \text{ s}}{\text{MF } \sqrt{\text{Re}_{s} (h^{*}/h_{e})^{0.18}}} \left[\frac{\mu^{*}/\mu_{e}}{\rho^{*}/\rho_{e}} \right]^{1/2}$$
 (24)

and

$$\frac{\delta^*}{\delta} = \frac{u_e^2/2h_e + 3.36 h_w/h_e - 0.376}{u_e^2/2h_e + 3.36 h_w/h_e + 5.79}$$
 (25)

and θ is obtained from an integration of the following equation, which is the result of combining the integral momentum and continuity equations:

$$\frac{d}{ds} (\rho_{e} u_{e}^{2} h) = \frac{C_{f}}{2} + \lambda - \frac{\delta^{*}}{u_{e}} \frac{du_{e}}{ds} + \delta \left[\frac{1}{u_{e}} \frac{du_{e}}{ds} + \frac{1}{\rho_{e} u_{e}^{2}} \frac{dP}{ds} \right]$$
(26)

The value of C_f, which is required in equation (26), is obtained (in the absence of mass addition) through the Reynolds analogy from Lee's relations for heat transfer rate, modified by the reference enthalpy method (20):

$$\dot{q} = \frac{0.354 \ \rho * \mu * \ u_e \ r_b \ (h_r - h_w)}{P_r \left[\int_0^s \rho * \mu * \ u_e \ r_b \ dS \right]^{1/2}}$$
(27)

At the higher of the two Reynolds numbers for which laminar data were available ($R_{\rm CQ} = 2.7 \times 10^6/{\rm ft}$), equations (24) and (25) consistently overpredict δ and δ^* (Figure 40). At the lower Reynolds number (0.67 x $10^6/{\rm ft}$) no consistent trend can be observed. Nor can one deduce any trend when comparing the momentum thickness given by equation (26) with values computed from measured data.

Because of the limited amount of experimental data available, no attempt is made to suggest improvements to the laminar correlations.

The effect of mass addition on momentum thickness is conputed in VIZAAD by first solving equation (26) for the zero mass addition case; then repeating the solution for θ , inserting the appropriate of $(\rho_V)_{\psi}$ in equation (26). The appropriate value of C_f for use in this solution is obtained from the relation (see Section 6):

$$\frac{C_{f}}{C_{fo}} = \frac{1}{1 + 0.663 \, \zeta} \tag{28}$$

The dependence of δ and δ on mass addition rate is deduced from the approximation:

FURTHER FOR THE STATES OF THE

$$\frac{\delta}{\delta_0} = \frac{\delta^*}{\delta^*_0} = \frac{\theta}{\theta_0} \tag{29}$$

The VIZAAD results are compared with test data in Figures 43 through 45 (solid lines). The method introduces a dependence on bluntness ratio. Agreement with measured data appears to be better for the sharp cone than for $R_{\rm N}/R_{\rm B}$ = 0.077.

The dependence on mass addition rate is introduced by McDonnell-Douglas (22) through the following relations:

$$\frac{\delta}{\delta_0} = \frac{\delta *}{\delta *} = \frac{\theta}{\theta} = \frac{C_f}{C_{fo}} + \zeta \tag{30}$$

where

$$\frac{C_f}{C_{fc}} = 1 + 0.68 \text{ W}^{0.4} \zeta + 0.08 \text{ W}^{0.4} \zeta^2$$
 (31)

and $W = \gamma_{inj.}/\gamma_{b.1.}$

In the present case the value of the ratio W was unity. Agreement with test data is good for the mass addition rates shown.

SECTION VI

SKIN FRICTION REDUCTION CORRELATION - LAMINAR FLOW

Sufficient data to assess the effect of mass injection on the skin friction reduction were not obtained in the experimental investigations (26,28) discussed in the body of this report. However, the laminar force data of Ref. 24 in conjunction with the large body of data of King (37) provide a suitable basis for reassessing the correlations which currently exist. Since the skin friction was not measured directly in the experiments, it was obtained indirectly by calculation as follows

$$C_{D_f} = C_{D_{TOTAL}} - \begin{bmatrix} C_{D_p} + C_{D_b} + C_{D_{inj.}} \end{bmatrix}$$
(32)

All drag coefficients are referenced to the cone base area. The total drag is the experimental value registered by the drag balance.

The pressure drag is defined as the streamwise component of force due to the slant-face pressure in excess of free stream pressure. This can be expressed as:

$$C_{D_{p}} = \frac{D_{p}}{1/2 \rho_{\infty} u_{\infty}^{2} A_{b}} = \frac{2 \pi \tan^{2} \theta_{b}}{1/2 \rho_{\infty} u_{\infty}^{2} A_{b}} \int_{0}^{L} (P-P_{\omega}) x dx$$
 (33)

The pressure, p, referred to here is the experimentally determined value.

The base drag corresponds to that which occurred in the experiment as a result of a particular method of mounting the models in the wind tunnel, and consequently has no significance beyond that of an experimental correction. Because the pressure existing on the base and inside the hollow afterbody was different from P_{ϖ} , a net force occurred on the model. The base drag coefficient can then be expressed as

$$C_{D_{b}} = -\frac{(P_{b} - P_{o}) A_{b}}{1/2 \rho_{o} u_{o}^{2} A_{b}}$$
(34)

The negative sign is inserted because pressure on the base actually produces a thrust on the model.

The passage of injected gas from the model surface into the boundary layer produces a drag force increment which is small, but not negligible. If we assume the validity of the no-slip boundary condition, then the injection velocity must be normal to the cone surface. The injection drag coefficient component may be computed from the flux of momentum across the porous surface as

$$C_{\text{Dinj.}} = \frac{\iint\limits_{A} (\rho v)_{w}^{2} / \rho_{w} \int \sin \theta_{b} dA_{s}}{1/2 \rho_{\infty} u_{\infty}^{2} A_{b}}$$
(35)

It is evident that the correction becomes more important at the higher injection rates, amounting to roughly 5% of the total drag at $\zeta \approx 3.0$.

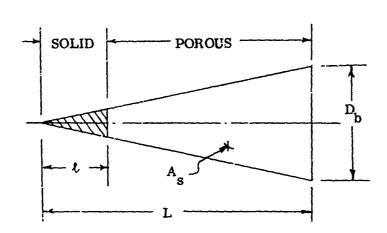
With the friction drag computed from equation (32), in conjunction with equations (33) to (35) the total skin friction coefficient \mathbf{C}_Γ can then be evaluated from the following relation:

$$C_{F} = C_{D_{f}} \frac{A_{b}}{A_{s} \cos \theta_{b}} \frac{q_{\infty}}{q_{e}}$$
(36)

or

$$C_{F} = C_{D_{f}} \frac{\tan \theta_{b}}{\left[1 - (\ell/L)^{2}\right]} \frac{q_{\infty}}{q_{e}}$$

where



Although the skin friction coefficient as deduced from equation (36) corresponds to the total skin friction of the cone, $C_{\rm F}$, the use of the data thereafter in correlation form are treated on a local basis, $C_{\rm F}$ (x), where

$$C_{F} = \frac{\iint_{A_{S}} C_{f} dA_{S}}{A_{S}}$$
(37)

Shown in Figure 46 are the data of King $^{(37)}$ plotted versus the blowing parameter, ζ . Data were obtained for two values of the free stream Mach number (i.e. $M_{\infty}=3.93$ and 5.64 or $M_{\rm e}=3.75$, 5.29) and for two injectant gases (i.e. Helium and air). The data for air injection show no apparent effect of free stream Mach number as is evident in the Helium data. In addition, it appears that Helium is not as effective as air in reducing the drag, which is in agreement with the conclusions of Little and Griffith $^{(36)}$. Also shown in Figure 46 is the data summary of Leadon et al $^{(39)}$ Kent, et al $^{(28)}$ and some unpublished GE data. The experimental results have been empirically curve-fitted using the equation for C_f/C_{f_0} derived in Dorrance $^{(40)}$, where

$$\frac{C_{f}}{C_{fo}} = \frac{\zeta}{e^{K \zeta_{-1}}}$$
(38)

expanding and retaining only linear terms in ζ , there results:

$$\frac{C_{f}}{C_{fo}} = \frac{1}{1 + K \zeta} \tag{39}$$

where K is the empirical constant that achieves a best fit with the data. It was concluded that

$$\frac{C_{f}}{C_{f0}} = \frac{1}{1 + 0.663 \, \zeta} \tag{40}$$

is a "best-fit" as shown in Figure 46.

The empirical techniques of Timmer et al $^{(22)}$ and Costello $^{(41)}$ are also shown in Fig. 46. It is evident that both of these methods tend to underpredict the skin friction drag of an ablating vehicle.

SUMMARY AND CONCLUSIONS

Measurements of pitot pressure and stagnation temperature profiles as well as surface pressures and temperatures obtained at AEDC under 1969 STREET-G and 1968 Mark 12 P/A contracts have been reduced and correlated. Values of boundary layer thickness, displacement and momentum thicknesses, form factor, profile exponents n and ϵ , and location of boundary layer transition have been deduced for turbulent boundary layers. In addition, the first three of these parameters have been deduced in several cases where boundary layer flow remained laminar.

The data treated in this study was obtained on a 7.25 degree sphere cone with bluntness ratios of zero, 0.077 and 0.180. Free stream Mach number was 8.0 and Reynolds number ranged from 0.65 x 10^6 to 3.7 x 10^6 per foot. Integrated mass addition ratio varied from zero to 0.05.

Results deduced from experiment are compared with empirical prediction methods used at General Electric, McDonnell-Douglas and Philco Ford. All three methods appear to overpredict the effect of mass addition on boundary layer thickness in turbulent flow. A new set of equations, accounting for the effect of mass addition on δ , δ , and θ is proposed for turbulent boundary layers. In addition, a correction is proposed to a constant used with the GE thickness predictions at zero mass addition. The proposed changes result in an improved drag and plasma attenuation prediction for flight vehicles.

In laminar boundary layers currently used correlations appear adequate at low mass addition rates. The quantity of available measured data was not adequate to permit an evaluation of currently used correlations at high mass addition rates.

In several turbulent cases measurements were compared with results computed with the GE Equilibrium Non-Similar Boundary Layer Program (ENSBL), a finite difference solution of the boundary layer equations. Three eddy viscosity models were used with ENSBL, and results computed with each are presented. Good agreement is noted in δ and δ^{\star} , but θ is slightly underpredicted by ENSBL.

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TABLE 1. KEY FOR BOUNDARY LAYER PROFILE DATA

A. TURBULENT

| Sym. | Ref. | Source Author | Model | M _{co} | Me | Re_/Ft. x 10 ⁻⁶ | $\frac{\dot{m}}{(\rho v)_{\infty} A_{b}}$ | ṁ(x) | Injectant | |
|----------------------|------|------------------------------|------------------|-----------------|-----|-------------------------------|--|---------------------------------------|----------------------|-----------------|
| 00400 | 26 | Martellucci | A B C D | Cone | 8 | 6.78 | 3.7 | 0 0.005 0.010 0.025 0.050 | Uni- form | N ₂ |
| \$ \D \D | 26 | Martellucci | F G H J | Cone | 8 | 6.78 | 2.7 | 0 0.005 0.010 0.025 | Uni- form | N ₂ |
| DD | 26 | Martellucci | M N | Cone | 8 | 6.78 | 2.7 | 0.010 0.025 | Non- uni- form | N ₂ |
| 東京大 | 28 | Kent, Martellucci, George | BB CC EE | Cone | 8 | 6.78 | 3.7 | 0.005 0.010 0.050 | Uni- form | co ₂ |
| Q Q | 28 | Kent, Martellucci, George | FF GG KK | Cone | 8 | 6.78 | 2.7 | 0 0.005 0.050 | Uni- form | N ₂ |
| • | 29 | Danberg | - | F.P. | 6.7 | 6.7 | - | - | Uni- form | Air |

B. LAMINAR

| Sym. | | Source | Model | M _∞ | R _N /R _B | Re Ft. | ḿ/ | | | |
|------|------|------------------------------|----------------|----------------|--------------------------------|--------|--------------------|----------------------------------|--------------|----------------|
| | Ref. | Author | Case | | 8 | RB | x 10 ⁻⁶ | (Pv) _∞ A _b | ṁ(x) | Injectant |
| 0 | 28 | Kent, Martellucci, George | PL QL | Cone | 8 | 0.077 | 2.7 | 0 0.050 | Uni- form | N ₂ |
| 0 | | | RL SL | | | 0.180 | | 0 0.050 | | |
| Q | 28 | Kent, Marteliucci, George | TL UL | Cone | 8 | 0 | 0.65 | 0.005 0.010 | Uni- form | N ₂ |
| 004 | | | VL WL XL | | | 0.077 | | 0 0.005 0.010 | | |

 $\frac{\text{TABLE 2}}{\text{DATA SUMMARY (REF. 26)}}$ $(\alpha = 0^{\circ})$

| _ | | | (α = | (*0 | | | |
|------|--|--|----------------|------|------|---|---|
| Case | Code | Group No. | Rem /Ft x 10-6 | m | m(x) | Profile Sta. x (inches) | Data Acquired |
| A | A0 A1 A2 A3 A4 A5 A6 | 33 3 58 96 101 102 107 | 3.7 | 0 | - | 41.51 36.61 30.61 21.61 14. 6 1 | Surface Pressure Force Profiles """""""""""""""""""""""""""""""""""" |
| В | B0 B1 B2 B3 B4 B5 B6 | 68 7 59 97 100 103 106 | 3.7 | .005 | 1111 | 41.51 36.61 30.61 21.61 14.61 | Surface Pressure Force Profiles """""""""""""""""""""""""""""""""""" |
| С | CO C1 C2 C3 C4 C5 C6 | 61 6 60 98 99 104 105 | 3.7 | .010 | 1111 | - 41 _* 51 36.61 30.61 21.61 14.61 | Surface Pressure Force Profiles """""""""""""""""""""""""""""""""""" |
| D | DO D1 D2 D3 D4 | 31 5 108 111 112 | 3.7 | .025 | 1111 | - 41.51 36.61 30.61 | Surface Pressure Force Profiles |
| E | E0 E1 E2 E3 E4 | 27 4 109 110 113 | 3.7 | .050 | 1111 | - 41.51 36.61 30.61 | Surface Pressure Force Prefiles |
| F | F0 F1 F2 F3 F4 F5 | 21 1 34 38 40 44 | 2.7 | 0 | - | - 41.51 36.61 30.61 21.61 | Surface Pressure Force Profiles "" |

TABLE 2 (Cont.)

| Case | Code | Group No. | R _{em} /Ft x 10 ⁻⁶ | H H | m(x) | Profile Sta. X (inches) | Data Acquired |
|------|----------------------------------|----------------------------------|---|------|------|---------------------------------------|--|
| G | G0 G1 G2 G3 G4 | 6 10 35 - 41 | 2.7 | .005 | 1111 | 41.51 30.61 | Surface Pressure Force Profiles |
| Н | HO H1 H2 H3 H4 H5 | 11 9 36 39 42 45 | 2.7 | .010 | 1111 | - 41.51 36.61 30.61 21.61 | Surface Pressure Force Profiles " |
| J | J0 J1 J2 J3 J4 | 16 8 37 - 43 | 2.7 | .025 | 1111 | - 41.51 30.61 | Surface Pressure Force Profiles |
| K | KO K1 | 22 2 | 2.7 | .050 | 1111 | - | Surface Pressure Force |
| L | LO L1 L2 | 69 11 85 | 2.7 | .005 | 1133 | - - 41.51 | Surface Pressure Force Profiles |
| М | но н1 н2 н3 н4 н5 | 74 12 86 87 88 91 | 2.7 | .010 | 1123 | \$1.51 36.61 30.61 21.61 | Surface Pressure Surface Pressure Force Profiles |
| N | NO N1 N2 N3 N4 | 82 13 89 - 90 | 2.7 | .025 | 1133 | 41.51 | Surface Pressure Force Profiles |

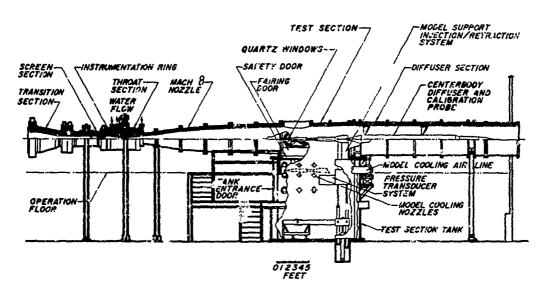
Table 3
Free Stream Conditions

 $M_{\infty} = 8.0$

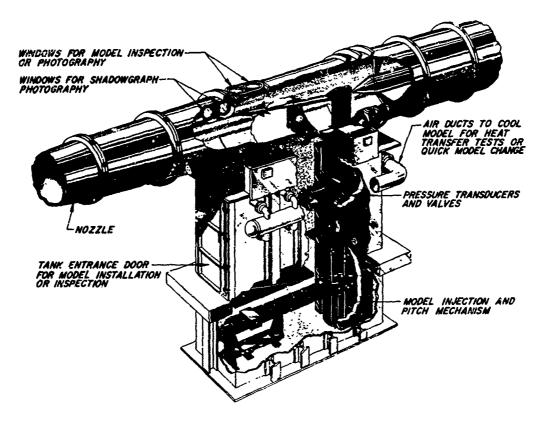
| Case | R _{e∞} x 10 ⁻⁶ per foot | Po psia | oR ^T o | P _m psia | ρ _∞ lbs/ft ³ | T • o _R | V ⇔ FPS | $\frac{\hat{\mathbf{m}}}{\hat{\mathbf{n}}} = \frac{\hat{\mathbf{m}} \mathbf{TOI}}{(\hat{\mathbf{n}}_{\mathbf{v}})_{\mathbf{s}} \mathbf{A}_{\mathbf{B}}}$ |
|---------------------|--|------------|-------------------|------------------------|---------------------------------------|-----------------------|------------|--|
| A | 3.69 | 849 | 1346 | .0870 | .00 2408 | 97.54 | 3871.4 | 0 |
| В | 3.70 | 850 | 1346 | .0872 | .00242 | 97.3 | 3865.0 | .0050 |
| С | 3.72 | 851 | 1337 | .0872 | .00242 | 97.2 | 3858.4 | .0091 |
| D | 3.70 | 851 | 1344 | .0871 | .00242 | 97.4 | 3869.0 | .0247 |
| E | 3.71 | 851 | 1344 | .0872 | .00242 | 97.4 | 3870.0 | .049 |
| F | 2.74 | 600 | 1303 | .062 | .00176 | 94.7 | 3810.0 | 0 |
| G | 2.74 | 598 | 1301 | .062 | .00176 | 94.49 | 3805.8 | .0043 |
| н | 2.75 | 601 | 1304 | .062 | .00177 | 94.71 | 3810.2 | .0091 |
| J | 2.76 | 602 | 1300 | .062 | .00178 | 94.4 | 3804.0 | .025 |
| м | 2.74 | 602 | 1308 | .0622 | .60177 | 95.0 | 3816.0 | .0090 |
| N | 2.73 | 500 | 1308 | .062 | .00176 | 95.1 | 3818.0 | .0249 |
| ě K | 2.74 | 600 | 1306 | •062 | .00176 | 94.9 | 3813.0 | .051 |
| Froff Froff K | 2.76 | 599 | 1302 | .062 | .00177 | 94.57 | 3807.3 | .0042 |

Table 4
Mass Addition Rate Schedule

| X/L | A | | Case C uss Addit | n | E | F | G | Case | s J | | T |
|------------|---|-------------|------------------------|----------|----------------|------|------------------|---------------------|--------------|--------|-------|
| 0 | | | | TON NACE | 8 | (OV) | #/ | Ft ² Sec | | M | N |
| 0 19 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | T_ | - | |
| 19 | | | | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 545 545 | | .00458 | | .02226 | .0443 .6787 | | .00277 | .00609 | .0166 | .00315 | .0086 |
| 747 | | .00927 | .0052 | .0457 | .0897 | | .00561 | .0123 | .0336 | .00639 | .0174 |
| 05 | | .00871 | .0160 | .0429 | .0842 .0328 | | .00527 | .0016 .00451 | .0315 | .0182 | .0491 |
| 00 | · | .00808 | .0149 | .0398 | .0782 .0334 | | .00489 .00209 | .0108 .00459 | .0293 | .0169 | •0456 |
| Fwd (pv) | 0 | .00608 | .0112 | .0300 | .0588 | 0 | .00368 | 00000 | | | .0194 |
| Aft | 0 | .00608 | .0112 | .0300 | .0588 | | | .00809 | <u>.0220</u> | .00419 | .0114 |
| m | 0 | .0050 | 0001 | | .0366 | 0 | .00368 | .00809 | .0220 | .0127 | .0343 |
| | | | .0091 | ,0247 | .049 | 0 | .0043 | .0091 | .0250 | .0090 | - 49 |



a. Tunnel Assembly



b. Tunnel Test Section

| TUNNEL PERFORMANCE | | | | | | | | | | | | |
|--------------------|-----------------|-----------|-----|---------|---------|-----|--------------------------|-----|--|--|--|--|
| Tunnel | Nominal Mach | Po (Psia) | | To (OR) | q (Ps18 | 1) | Re/ft. x10 ⁻⁶ | | | | | |
| | Number_ | Min | Max | Max | Min | Max | Min | Max | | | | |
| В | 6 | 20 | 300 | 1350 | 0.3 | 4.6 | 0.3 | 5.3 | | | | |
| | 8 | 50 | 900 | 1350 | 0.3 | 4.1 | 0.3 | 3.8 | | | | |

Figure 1. Tunnel Layout and Performance Characteristics

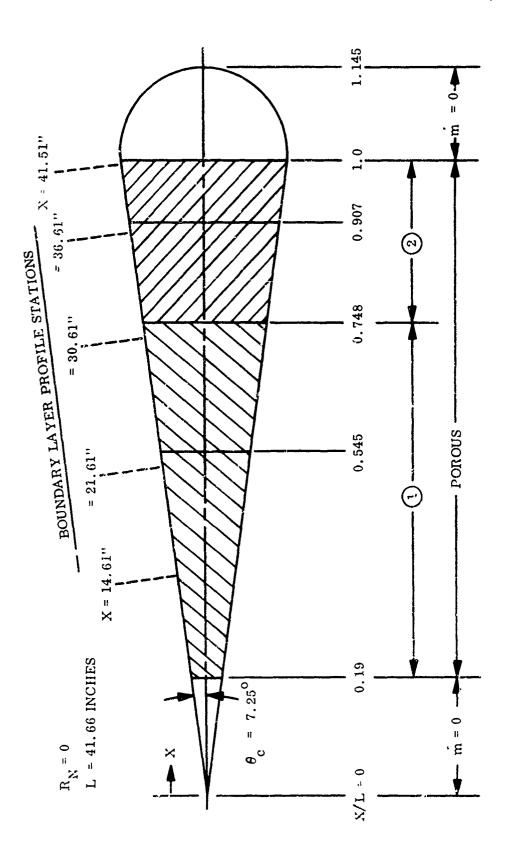


Figure 2. Schemalic Drawing of the Model Configuration

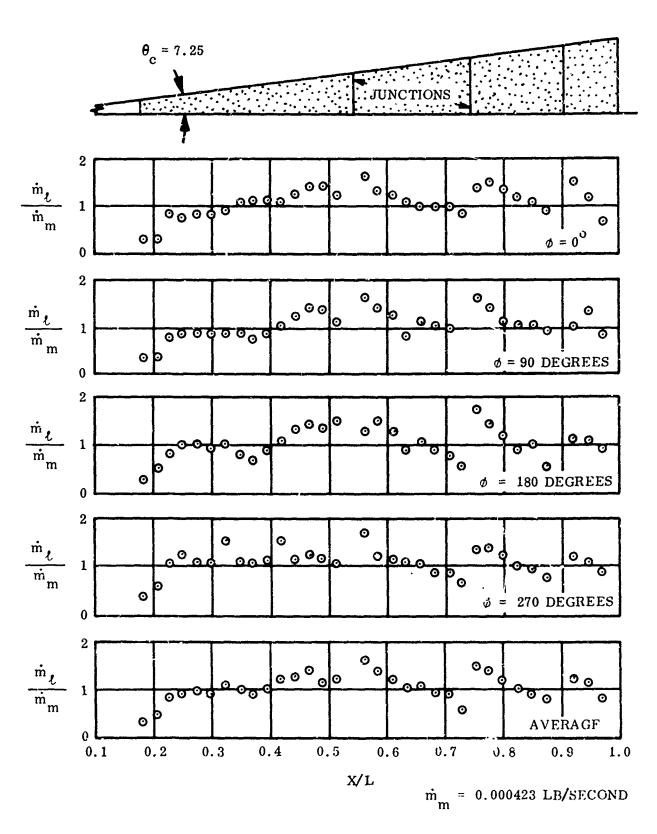


Figure 3. Surveys of the Local Mass Flow Rates - Axial Variation

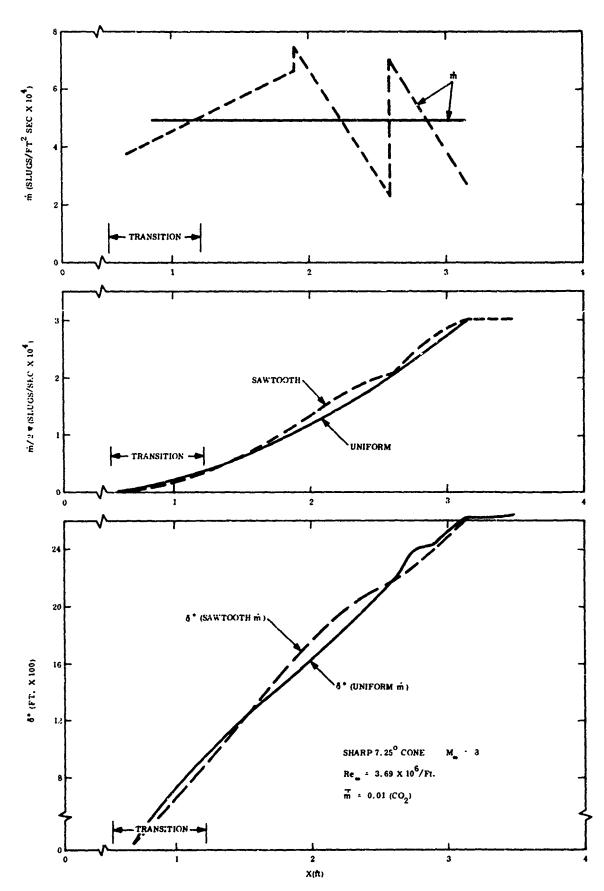


Figure 4. Displacement Thickness and Mass Addition Rate (ENSBL Calculation)

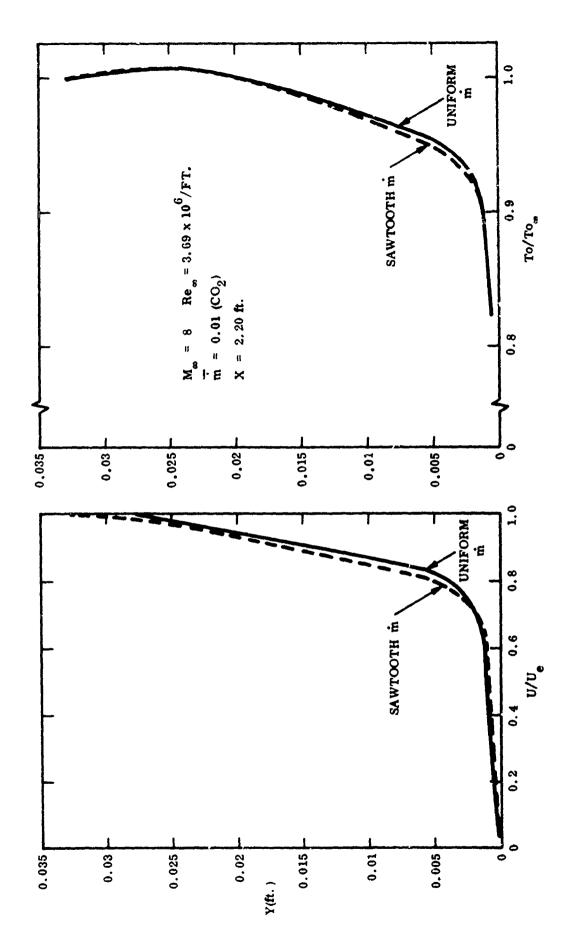


Figure 5. Profile Comparison at Station Where Difference in in Rate is Greatest (ENSBL Calculation)

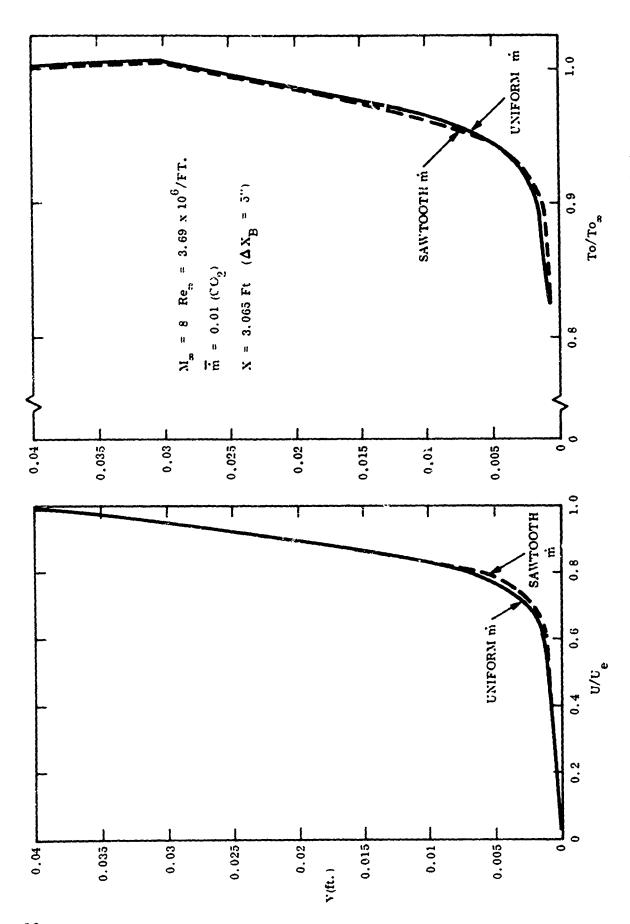
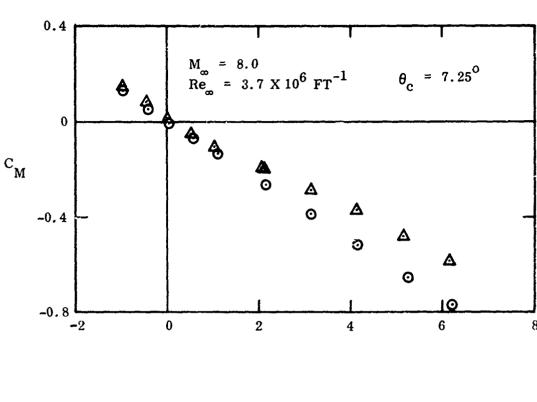


Figure 6. Profile Comparison at a Station Where Total Mass Added is Identical (ENSBL Calculation)



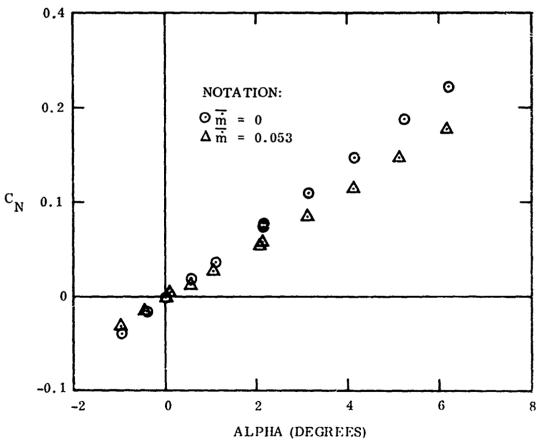


Figure 7. Pitching Moment and Normal Force Coefficients

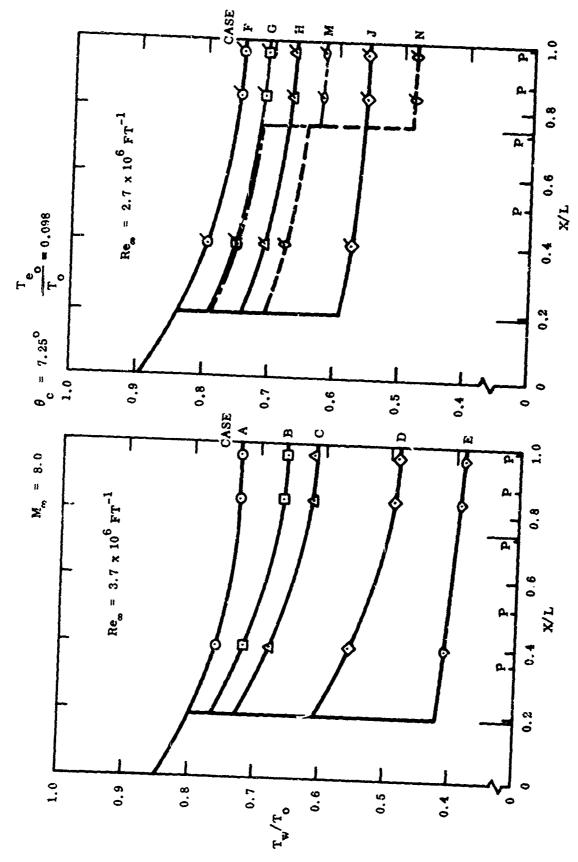


Figure 8. Wall Temperature Distribution

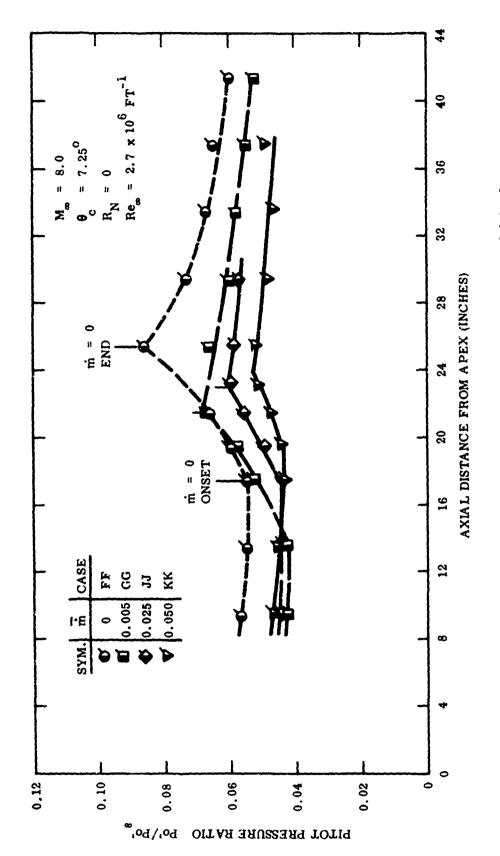
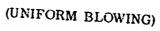


Figure 9. Transition Detection from Pitot Pressure Survey on Model Surface



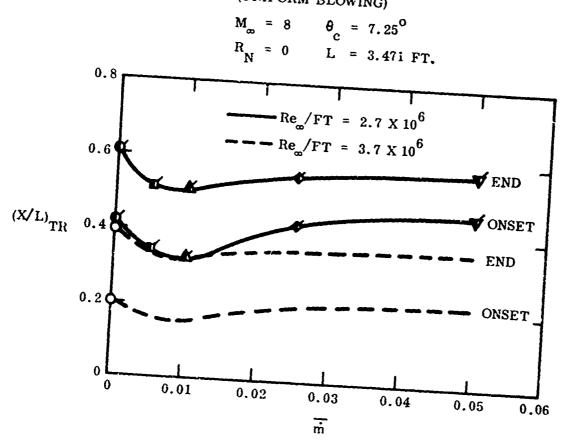


Figure 10. Transition Location vs Mass Addition Rate

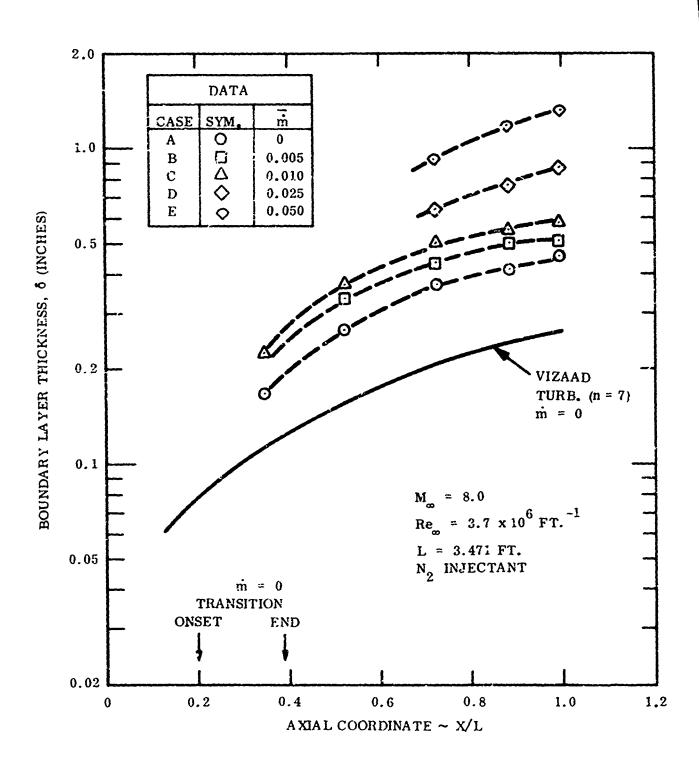


Figure 11. Effect of Mass Addition on the Boundary Layer Thickness of a Sharp 7.25° Half Angle Cone (Re $_\infty$ = 3.7 x 10 6 ft⁻¹)

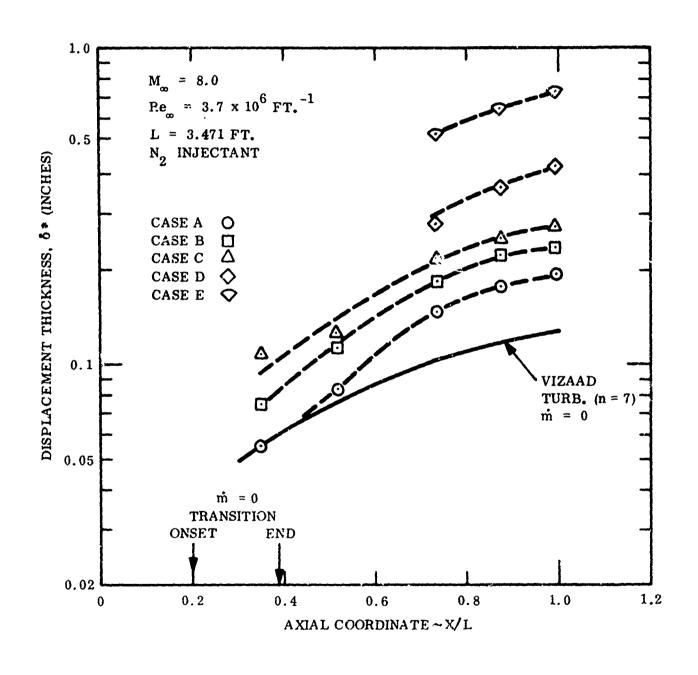


Figure 12. Effect of Mass Addition on the Displacement Thickness of a Sharp 7.25° Half Angle Cone (Re_{∞} = 3.7 x 10^{6} ft⁻¹)

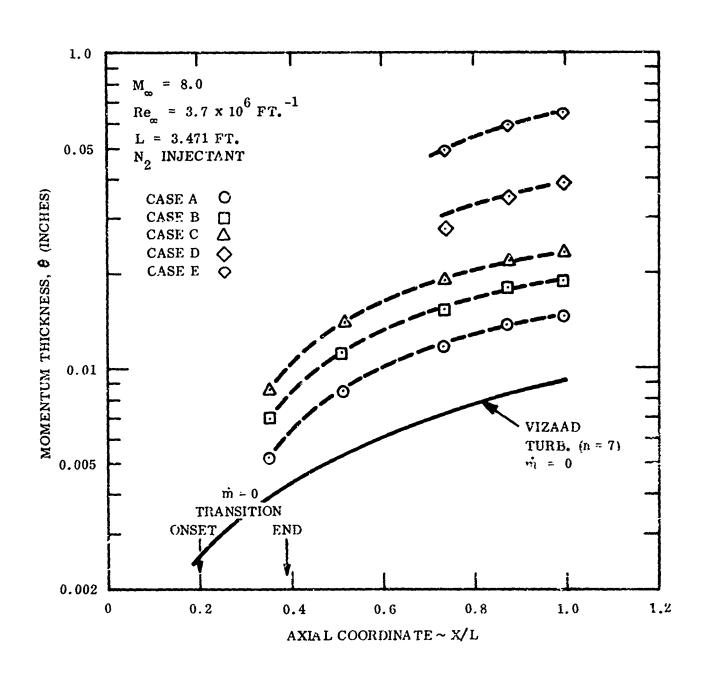


Figure 13. Effect of Mass Addition on the Momentum Thickness of a Sharp 7.25° Half Angle Cone ($\text{Re}_{\infty} = 3.7 \times 10^6 \text{ ft}^{-1}$)

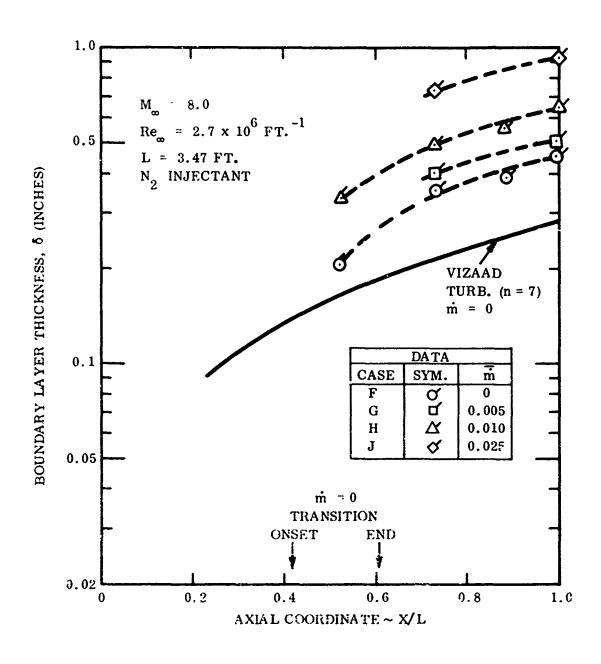


Figure 14. Effect of Mass Addition on the Boundary Layer Thickness of a Sharp 7.25° Half Angle Cone (${\rm Re}_{\infty}$ = 2.7 x 10° ft⁻¹)

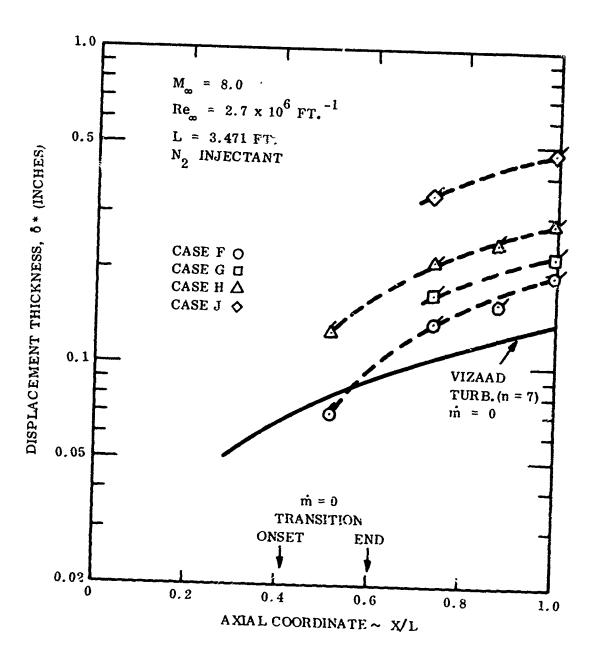


Figure 15. Effect of Mass Addition on the Displacement Thickness of a Sharp 7.25° Half Angle Cone ($Re_{\infty} = 2.7 \times 10^6 \text{ ft}^{-1}$)

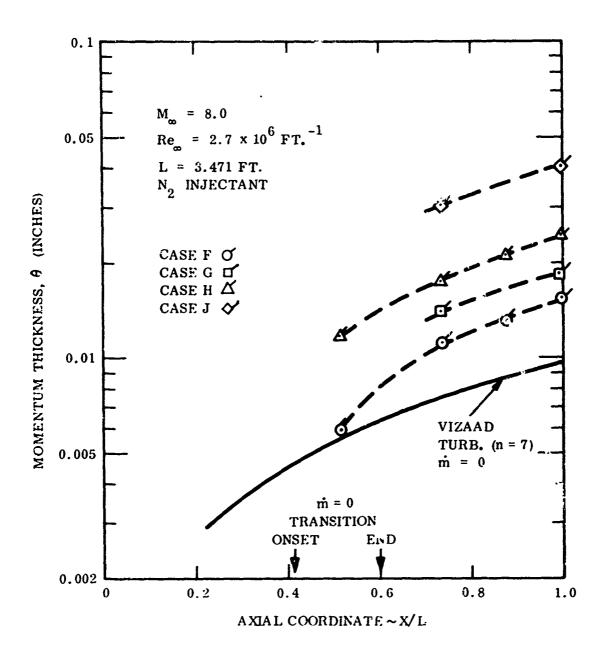


Figure 16. Effect of Mass Addition on the Momentum Thickness of a Sharp 7.25° Half Angle Cone (Re $_{\infty}$ = 2.7 x 10 6 ft⁻¹)

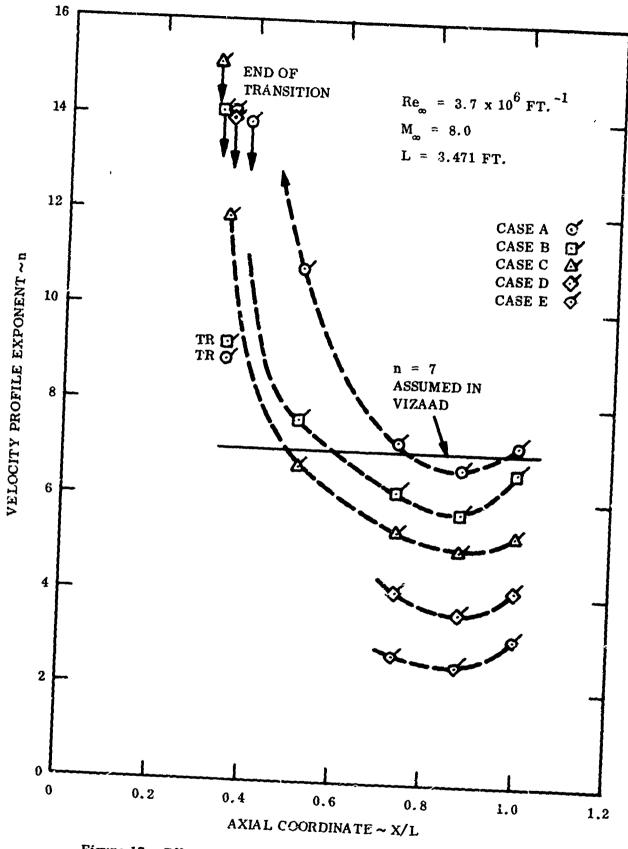


Figure 17. Effect of Mass Addition on Velocity Profile Exponent $(Re_{\infty} = 3.7 \times 10^6 \text{ ft}^{-1})$

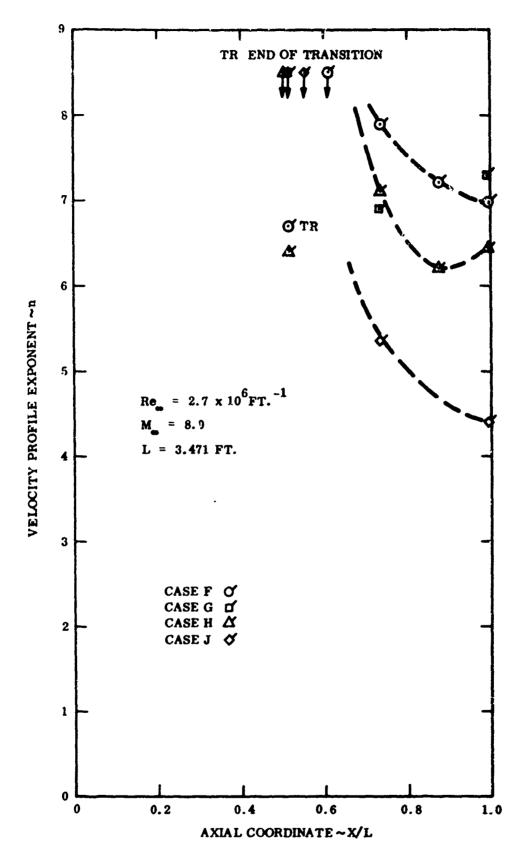


Figure 18. Effect of Mass Addition on Velocity Profile Exponent ($Re_{\infty} = 2.7 \times 10^6 \text{ ft}^{-1}$)

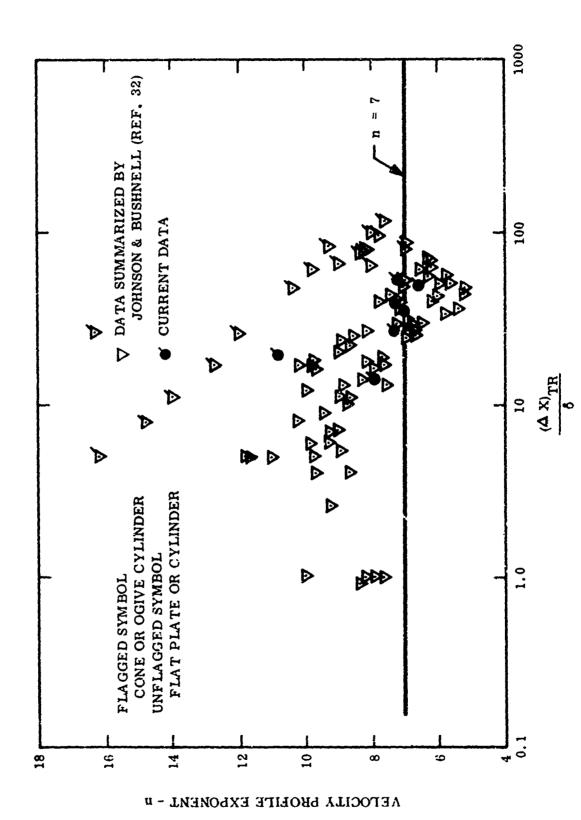


Figure 19. Variation of Velocity Profile Exponent with Normalized Length from End of Transition

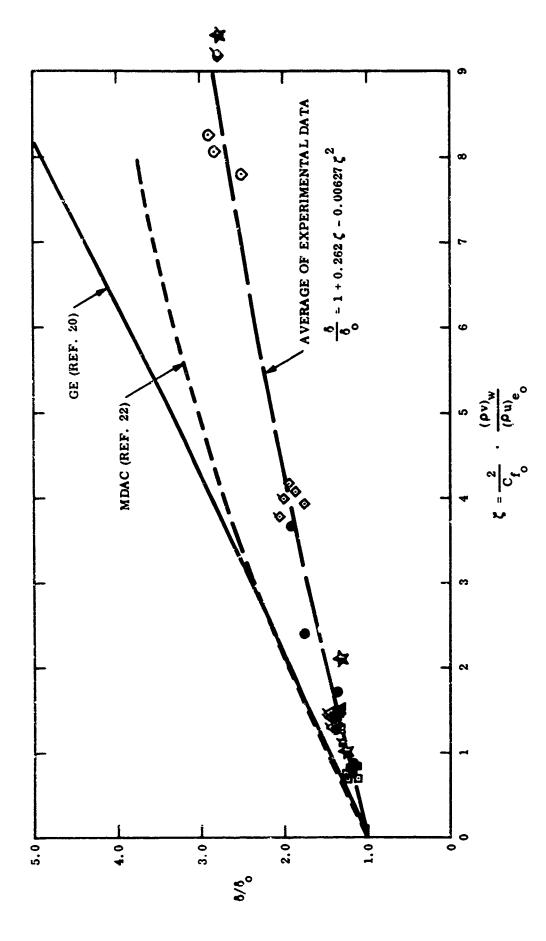
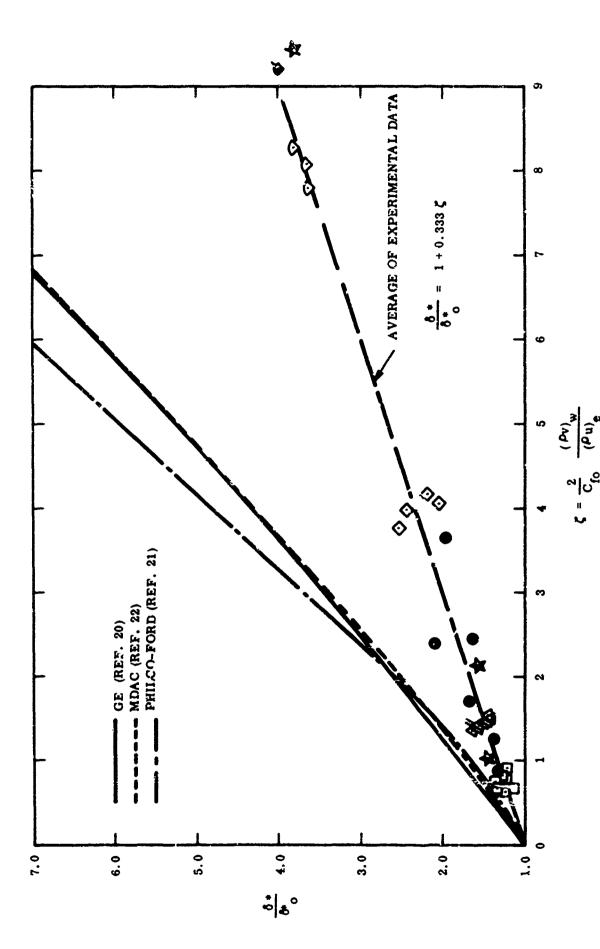


Figure 20. Effect of Mass Addition on Boundary Layer Thickness (Turbulent)



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Figure 21. Effect of Mass Addition on Displacement Thickness (Turbulent)

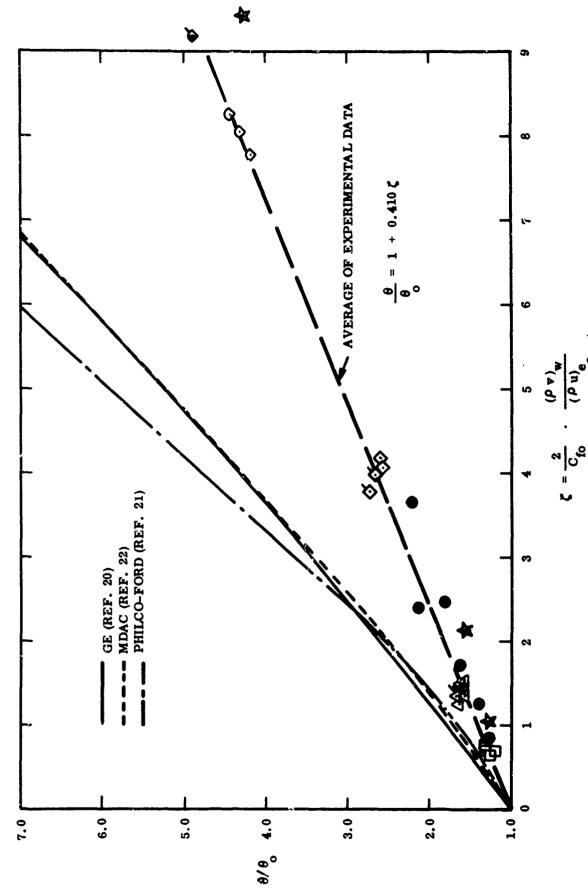


Figure 22. Effect of Mass Addition on Momentum Thickness (Turbulent)

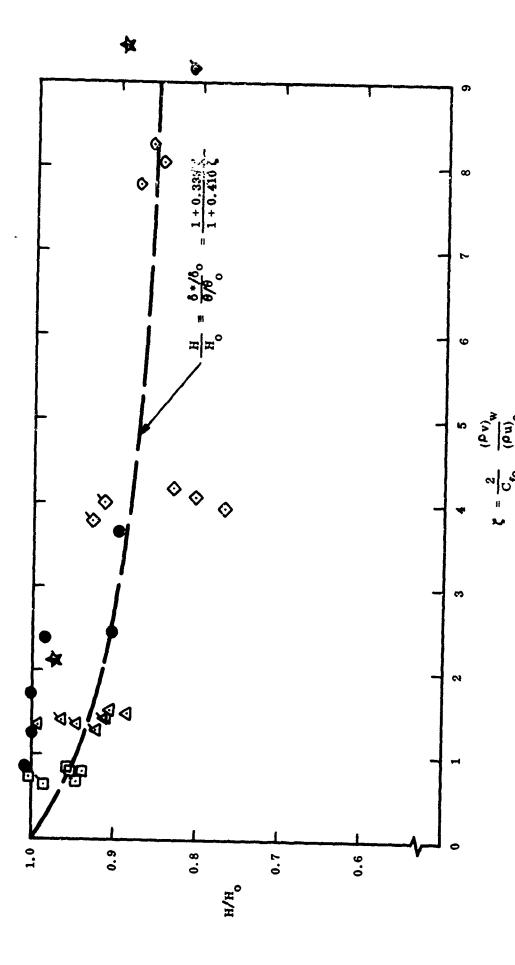


Figure 23. Effect of Mass Addition on the Form Factor - $H = \delta * / \theta$ (Turbulent)

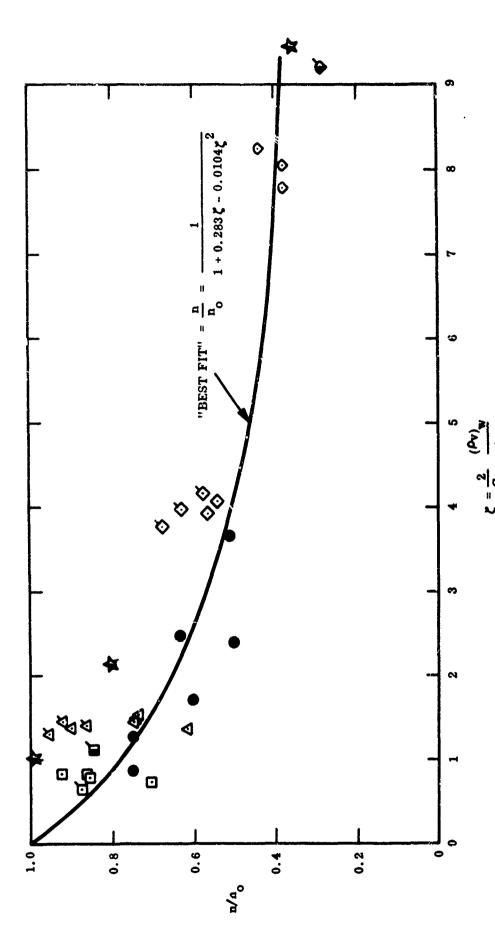
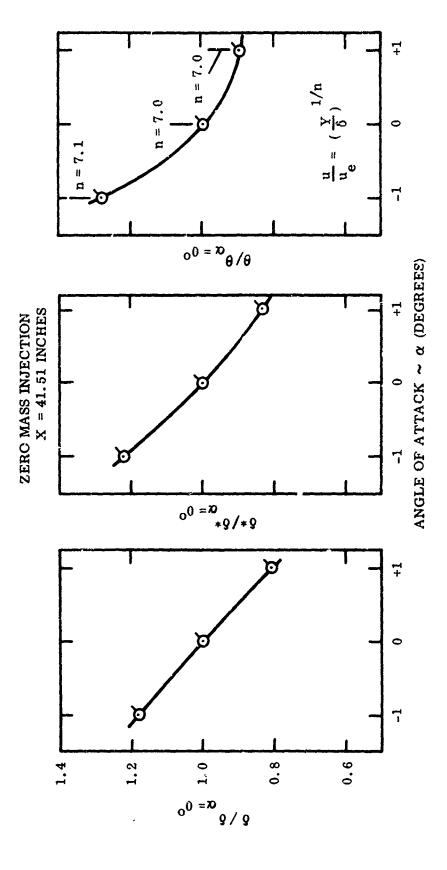


Figure 24. Effect of Mass Addition on Velocity Profile Exponent - n



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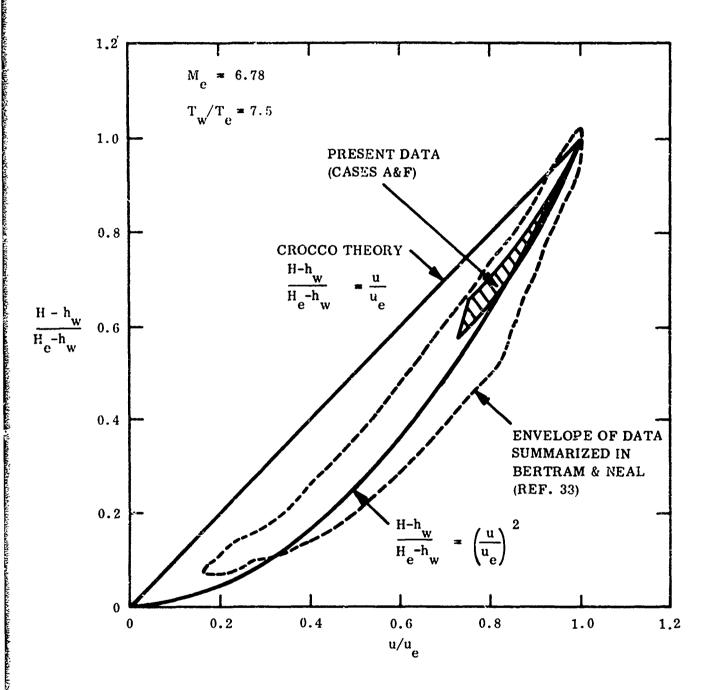


Figure 26. Comparison of Total Enthalpy Profile with Crocco Theory (Zero Mass Injection)

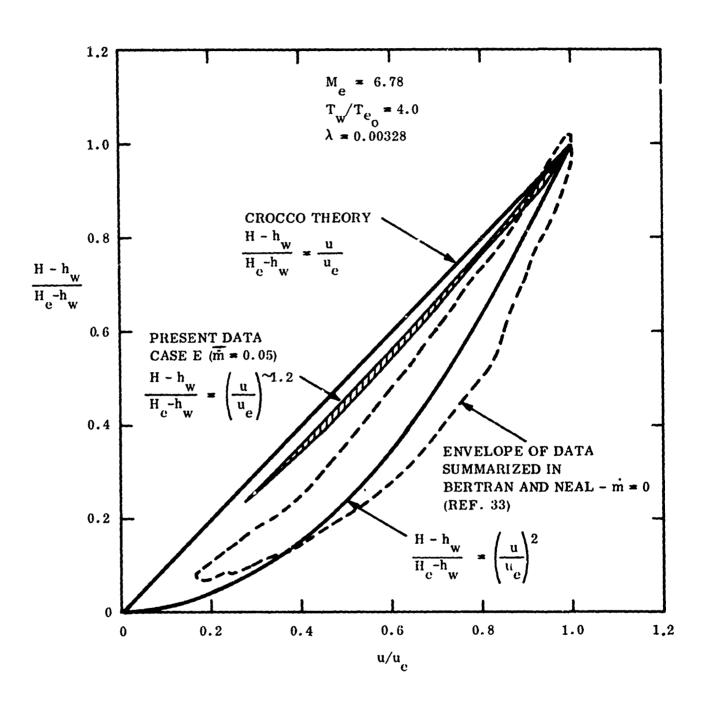


Figure 27. Comparison of Total Enthalpy Profile with Crocco Theory (Effect of Mass Injection)

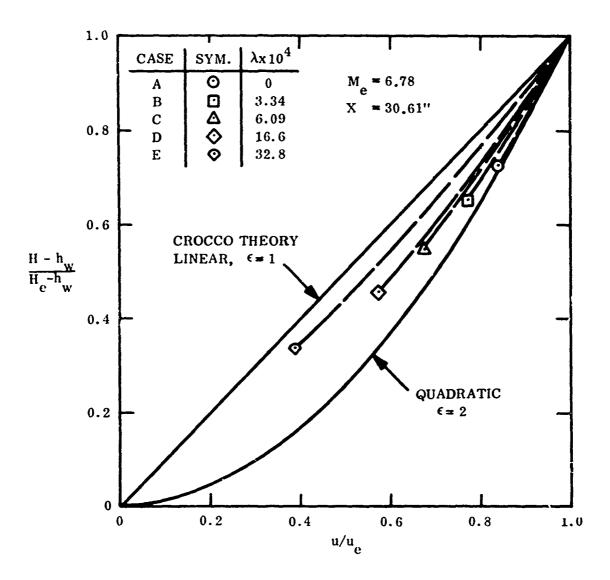
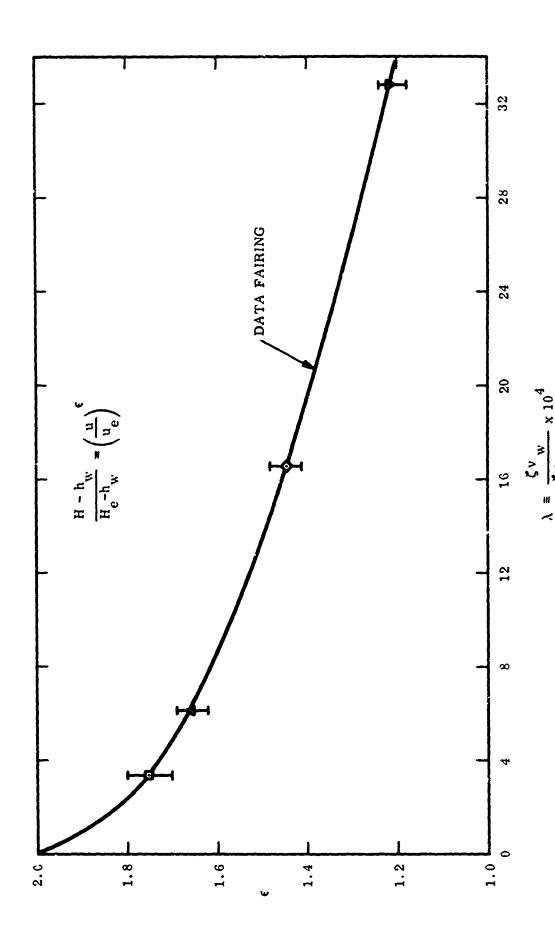


Figure 28. Effect of Mass Injection on Total Enthalpy Profile



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Figure 29. Effect of Mass Injection on Exponent in Total Futhalpy Relation

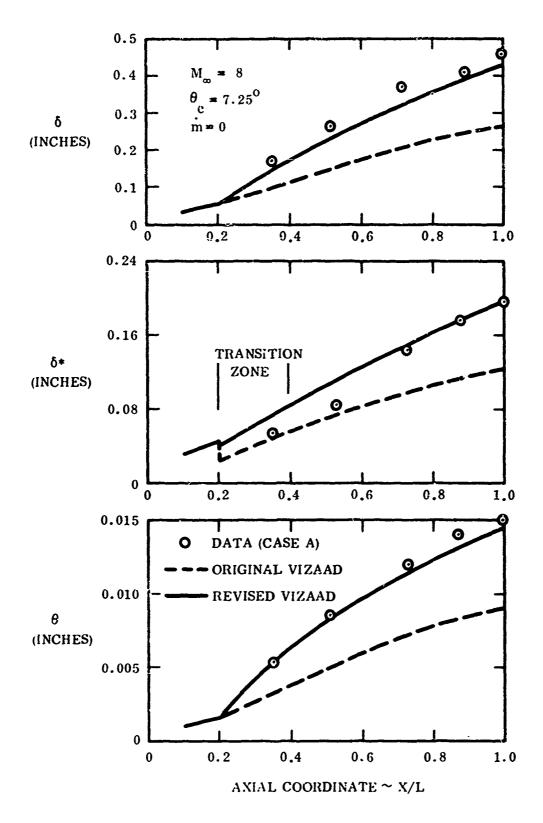


Figure 30. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Case A)

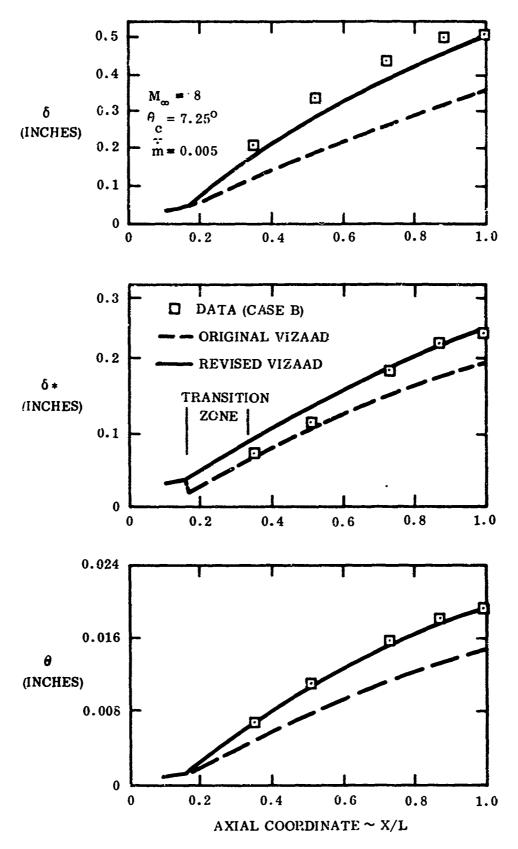


Figure 31. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Case B)

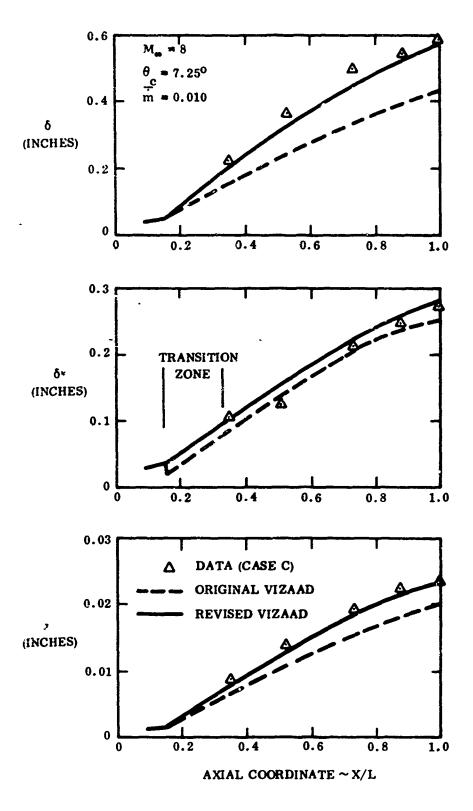


Figure 32. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Case C)

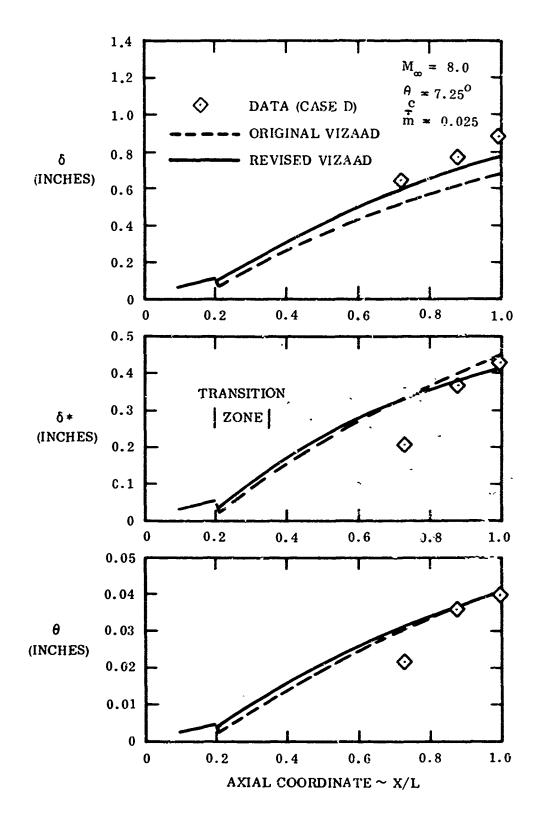


Figure 33. Comparison of Theory with Experimental Viscous Layer Thicknesses (Case D)

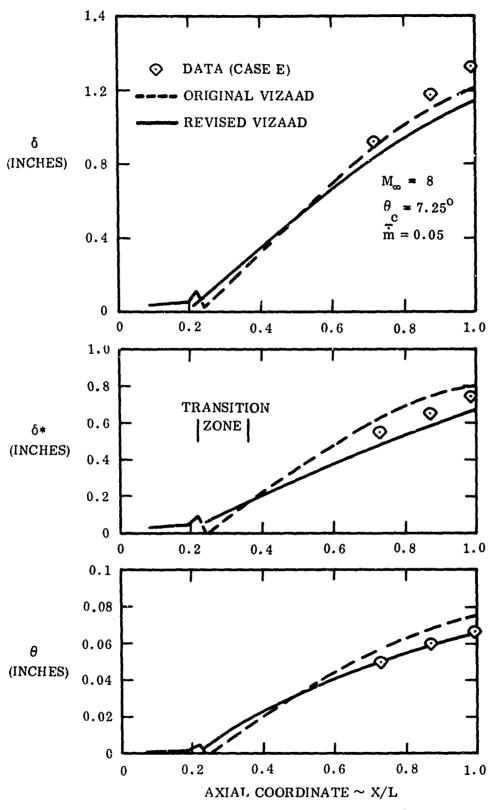


Figure 34. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Case E)

PLASMA ATTENUATION

Figure 35. Slender (R/V) S Band Plasma Attenuation

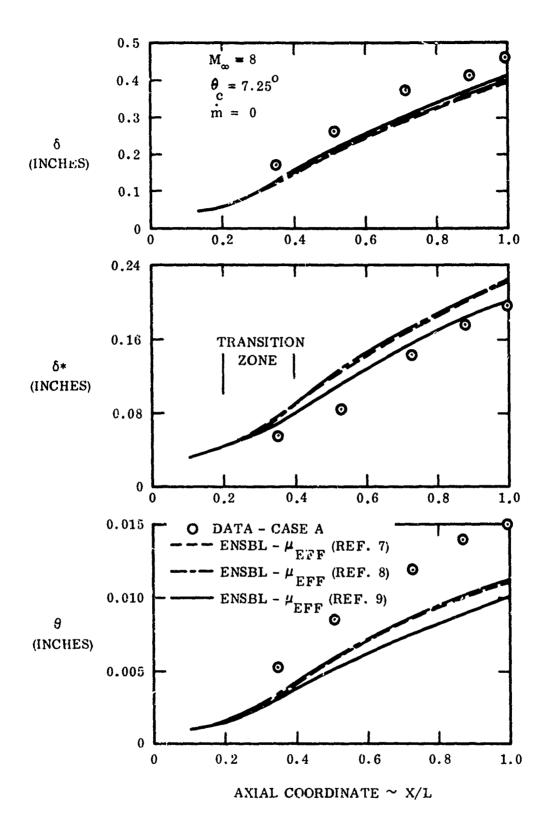


Figure 36. Comparison of ENSBL Program Results with Experimental Data

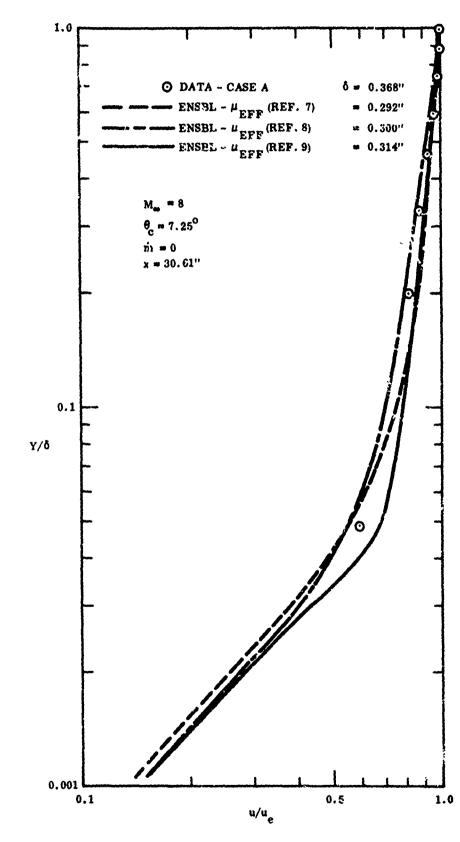


Figure 37. Profile Comparison of ENSBL Program Results with Data

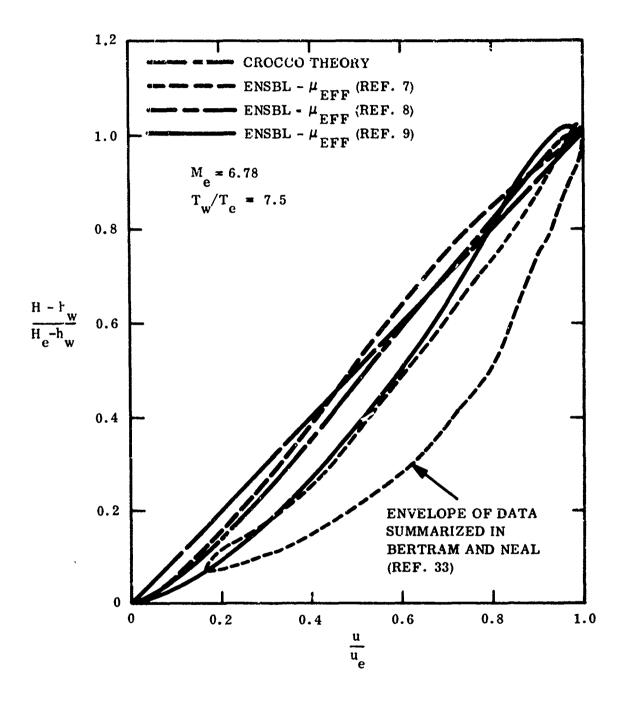


Figure 38. Comparison of Predicted Enthalpy Profiles with Crocco Theory and Data - Zero Mass Injection

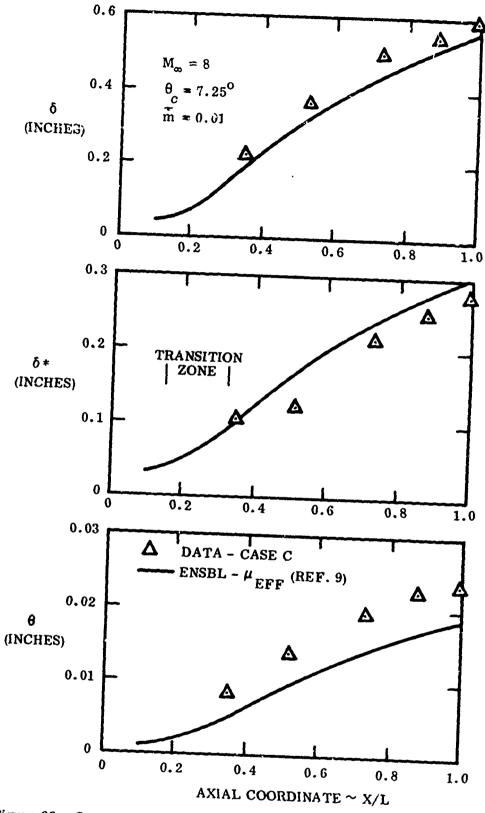


Figure 39. Comparison of ENSBL Program Results with Experimental Data

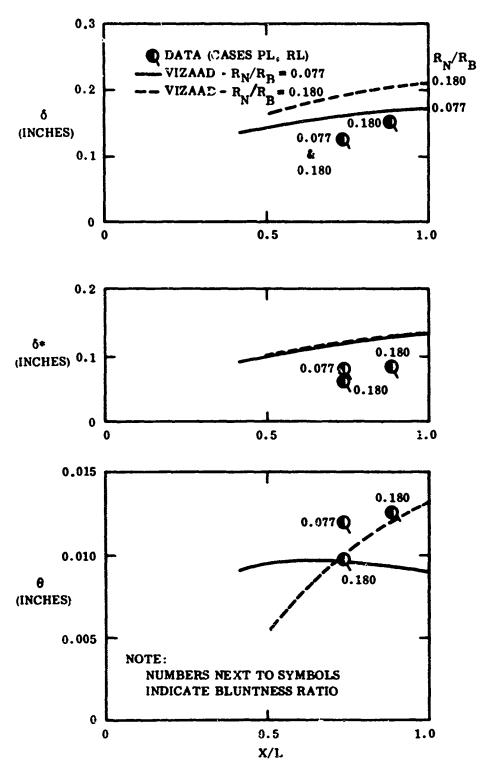


Figure 40. Comparison of Theory with Experimental Viscous Layer Thicknesses (Laminar)

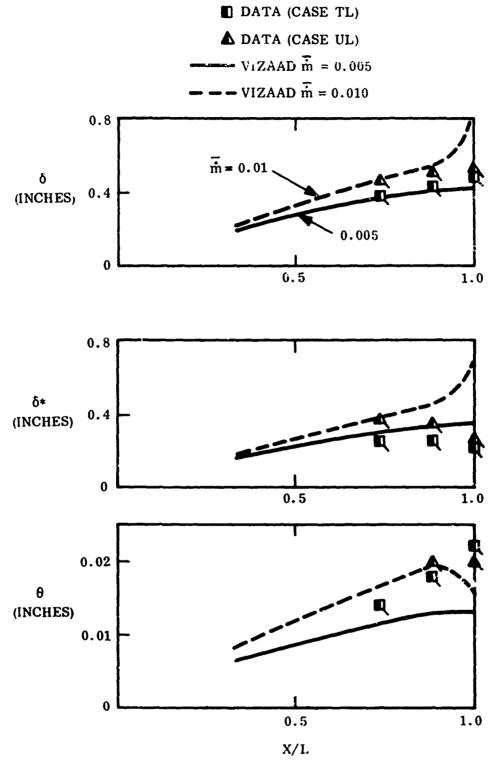


Figure 41. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Laminar)

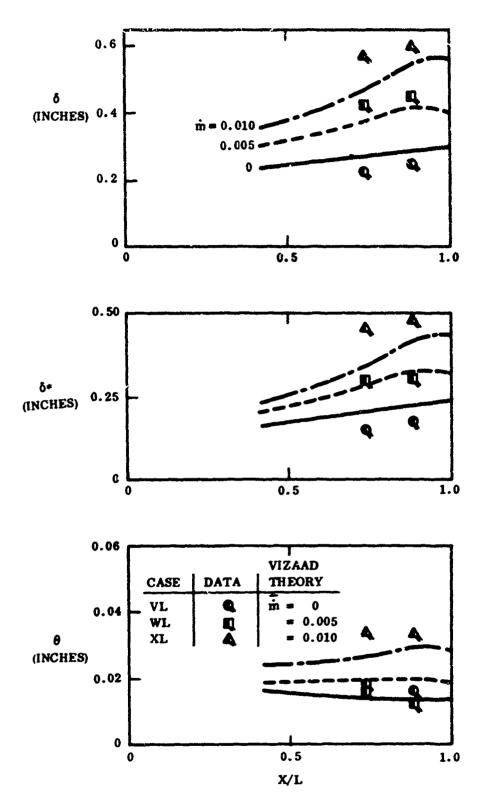
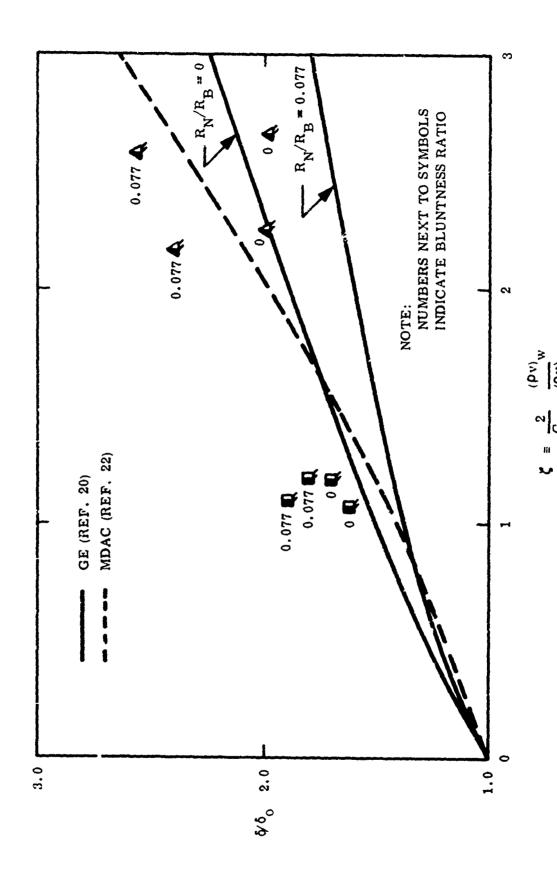


Figure 42. Comparison of Theory with Experimental Viscous Layer
Thicknesses (Laminar)



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Figure 43. Effect of Muss Addition on Boundary Layer Thickness (Laminar)

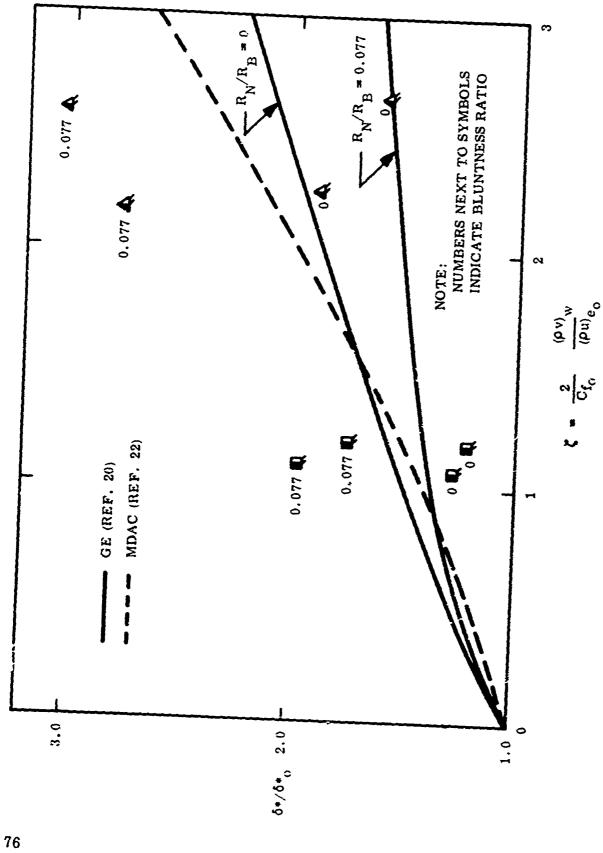


Figure 44. Effect of Mass Addition on Displacement Thickness (Laminar)

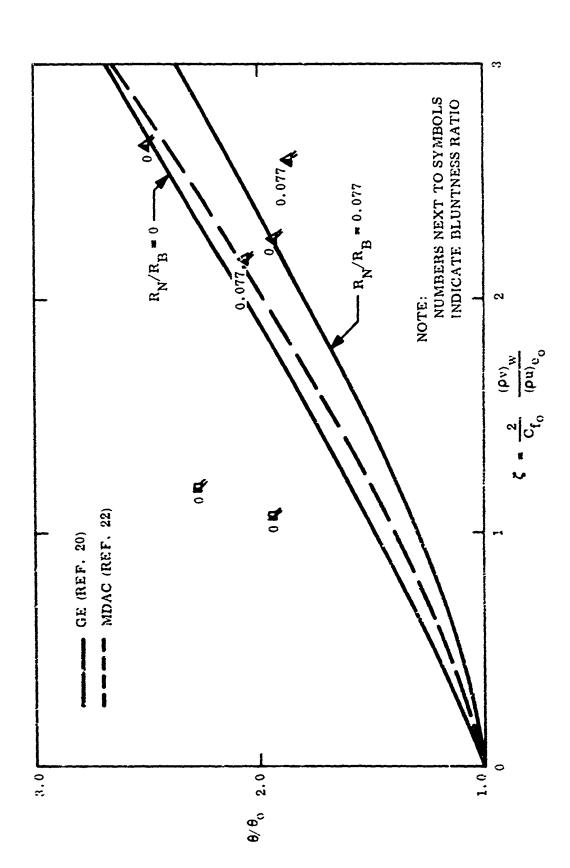


Figure 45. Effect of Mass Addition on Momentum Thickness (Laminar)

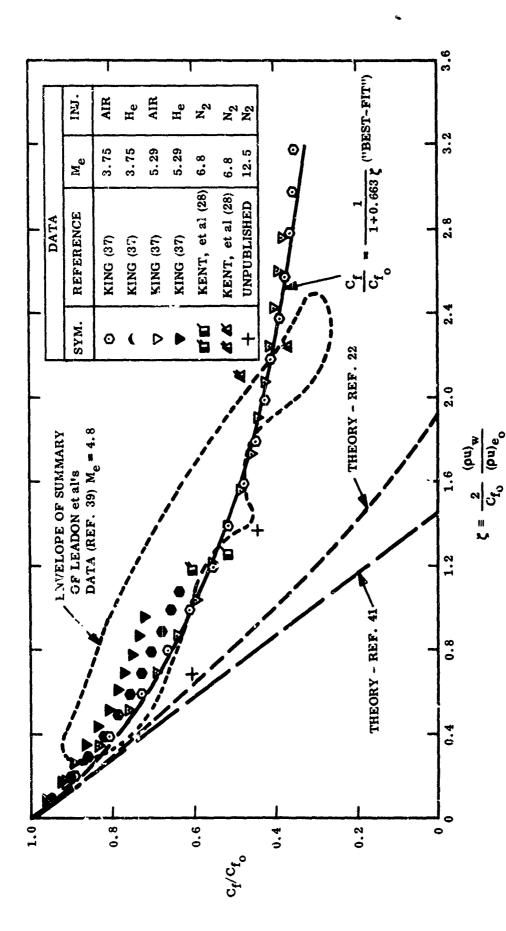


Figure 46. Effect of Mass Injection on Skin Friction Reduction - Laminar

APPENDIX A

TABULATED SUMMARY OF PROFILE DATA BOUNDARY LAYER DATA DEDUCED FROM PROFILES

| M _∞ ≈ 8 θ c = 7.25° | CASE A | | | | | | |
|--|------------------------|--------|-------|-------|-------|--|--|
| N ₂ - Injectant | AXIAL STATION (INCHES) | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| ke ₈ x 10 ⁻⁶ | 6.63 | 9.24 | 13.3 | 16.0 | 18.2 | | |
| (Pu) LBM DFT ² SEC | 18.3 | 18.3 | 18.3 | 18.3 | 18.3 | | |
| (pv) LBM FT ² SEC | 0 | 0 | 0 | 0 | 0 | | |
| $\lambda \equiv (\rho v)_{w} / (\rho u)_{e_{0}} \times 10^{4}$ | 0 | 0 | 0 | 0 | 0 | | |
| Cf _o (THEOR.) × 10 ³ | .9561 | .8949 | .8415 | .8133 | .7935 | | |
| $\zeta = \frac{2}{Cf_0}\lambda$ (Theor.) | 0 | 0 | 0 | O | 0 | | |
| δ _o (INCHES) | .173 | .270 | .368 | .415 | .455 | | |
| δ* (INCHES) | .0554 | .0832 | .148 | .178 | .194 | | |
| θ _o (INCHES) | .00529 | .00856 | .0119 | .0139 | .0149 | | |
| $H_0 = \delta_0^* / \theta_C$ | 10.47 | 9.72 | 12.44 | 12.80 | 13.02 | | |
| n (velocity profile exponent) | 8.9 | 10.8 | 7.2 | 6,65 | 7.15 | | |
| δ / δ _ο | | | | | | | |
| δ*/ δ*ο | | | | | | | |
| θ / θο | | | X | | | | |
| н/н _о | | | | | | | |
| n/n ₀ | | | | | | | |
| Tw/Teo | 7.85 | 7.62 | 7.48 | 7.46 | 7.45 | | |
| P _W /P ₆₀ | 2.80 | 3.00 | 2.80 | 2.86 | 2.81 | | |

| M _∞ = 8 | | | CASE _ | В | |
|--|----------------|----------------|----------|--------|--------|
| $\theta_{\rm c} = 7.25^{\circ}$ | <u></u> | | | | |
| N ₂ - Injectant | ļ | AXIAL STA | TION (IN | CHES) | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res x 10 ⁻⁵ | 6.63 | 9.24 | 13.3 | 16.0 | 18.2 |
| (Pu) LBM FT ² SEC | 18.3 | 18.3 | 18.3 | 18.3 | 18.3 |
| (OV) LBM W FT ² SEC | .00612 | .00612 | .00612 | .00612 | .00612 |
| $\lambda \equiv (\rho_{\rm V})_{\rm W} / (\rho_{\rm U})_{\rm e_{\rm O}} \times 10^4$ | 3.344 | 3 .3 44 | 3.344 | 3.344 | 3.344 |
| Cf _o (THEOR.) × 10 ³ | .9561 | .8949 | .8415 | .8133 | .7935 |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | .700 | .747 | .795 | .822 | .843 |
| δ (INCHES) | . ∶2 16 | .340 | .440 | .510 | .515 |
| δ * (INCHES) | .0743 | .112 | .182 | .223 | .238 |
| θ (INCHES) | .00701 | .0112 | .0156 | .0183 | .0191 |
| H = δ*/θ | 10.60 | 10.00 | 11.67 | 12.19 | 12.46 |
| n (velocity profile exponent) | 9.25 | 7.65 | 6.15 | 5.75 | 6.60 |
| δ/δ ₀ | 1.25 | 1.26 | 1.195 | 1.23 | 1.132 |
| 5*/ 5*° | 1.341 | 1.346 | 1.230 | 1.253 | 1.227 |
| θ/θ。 | 1.325 | 1.308 | 1,311 | 1.317 | 1.282 |
| н/н _о | 1.014 | 1.03 | .938 | .952 | .957 |
| n/n _o | 1.04 | .708 | .854 | .865 | .924 |
| T _w /Teo | 7.44 | 7.12 | 6.85 | 6.75 | 6.73 |
| P _w /P _∞ | 2.91 | 2.92 | 2.90 | 2.90 | 2.80 |

 $\theta_{c} = 7.25^{\circ}$

| N_2 - Injectant | AXIAL STATION (INCHES) | | | | | | |
|---|------------------------|--------|--------|--------|--------------|--|--|
| ng - injectant | 14.61 | 21.61 | 30.61 | 36.61 | (1, 51 | | |
| 6 | 14.01 | 21.01 | 30.01 | 30.01 | 41.51 | | |
| Res x 10 ⁻⁶ | 6.63 | 9.24 | 13.3 | 16.0 | 18.2 | | |
| (O u)eo LBM FTZSEC | 18.3 | 18.3 | 18.3 | 18.3 | 18.3 | | |
| (Ov) _w LBM FT ² SEC | .01115 | .01115 | .01115 | .01115 | .01115 | | |
| $\lambda = (ov)_{w} / (ou)_{e_0} \times 10^4$ | 6.093 | 6.093 | 6.093 | 6.093 | 6.093 | | |
| Cf _o (THEOR.) × 10 ³ | .9561 | .8949 | .8415 | .8133 | .7935 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | 1.274 | 1.362 | 1.448 | 1.498 | 1.536 | | |
| δ (INCHES) | .230 | .378 | .505 | .558 | •595 | | |
| δ* (INCHES) | .1085 | .137 | .218 | .251 | . 277 | | |
| θ (INCHES) | .00866 | .0142 | .0193 | .0222 | .0235 | | |
| H = 6*/0 | 12.53 | 9.65 | 11.30 | 11.30 | 11.79 | | |
| n (velocity profile exponent) | 11.9 | 6.65 | 5.35 | 4.95 | 5.25 | | |
| δ/δο | 1.33 | 1.40 | 1.372 | 1.345 | 1.310 | | |
| δ*/ δ*ο | 1.958 | 1.647 | 1.473 | 1.410 | 1.428 | | |
| θ/θο | 1.637 | 1.659 | 1:622 | 1.600 | 1.577 | | |
| н/н _о | 1.20 | .993 | .908 | .883 | .905 | | |
| n/n _o | 1.39 | .615 | .743 | .745 | .735 | | |
| T _w /Te _o | 7.02 | 6.70 | 6.42 | 6.31 | 6.27 | | |
| P _W /P _∞ | 2.93 | 2.95 | 2.95 | 2.95 | 2.85 | | |

M = 0

CASE D

| $\theta_{\rm c} = 7.25^{\rm o}$ | | | | | | | |
|---|-------|----------|-----------|---------------|--------------|--|--|
| N_2 - Injectant | | AXIAL ST | ATION (IN | CHES) | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| Res x 10 ⁻⁶ | 6.63 | 9.24 | 13.3 | 16.0 | 18,2 | | |
| (O u)eo LBM FT ² SEC | 18.3 | 18.3 | 18.3 | 1 8 ≩3 | 18.3 | | |
| (PV) LBM FT ² SEC | .0303 | .0303 | .0303 | .0303 | .0303 | | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_{O}} \times 10^{4}$ | 16.56 | 16.56 | 16.56 | 16.56 | 16.56 | | |
| Cf _o (THEOR.) × 10 ³ | .9561 | .8949 | .8415 | .8133 | .7935 | | |
| $ \zeta = \frac{2}{C f_0} \lambda $ (THEOR.) | 3.463 | 3.700 | 3.935 | 4.072 | 4.173 | | |
| δ (INCHES) | - | - | .650 | .775 | . 885 | | |
| δ * (INCHES) | - | - | .209 | .3 65 | .425 | | |
| θ (INCHES) | - | - | .0219 | .0355 | .0393 | | |
| $H = \delta^*/\theta$ | - | - | 9.54 | 10.28 | 10.8 | | |
| n (velocity profile exponent) | - | •• | 4.05 | 3.6 | 4.1 | | |
| 8/5 ₀ | | | 1.766 | 1.87 | 1.945 | | |
| δ*/ δ° ₀ | | | 1.412 | 2.051 | 2.196 | | |
| θ/θ _ο | | | 1.840 | 2.554 | 2.640 | | |
| н/но | | | .767 | .803 | .830 | | |
| n/n _o | | | .563 | .541 | .573 | | |
| T _w /Te _O | | | 5,12 | 5.01 | 4.96 | | |
| P _w /P _∞ | | | 2.86 | 2.82 | 2.74 | | |

| M _m = 8 θ _c = 7.25° | CASE E | | | | | | | |
|--|--------|------------------------|-------|-------|-------|--|--|--|
| N ₂ - Injectant | | AXIAL STATION (INCHES) | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | | |
| Res x 10 ⁻⁶ | 6.63 | 9.24 | 13.3 | 16.0 | 18.2 | | | |
| (P u) LBM eo FT ² SEC | 18.3 | 18.3 | 18.3 | 18.3 | 18.3 | | | |
| (ρ v) LBM FT ² SEC | .060 | .060 | •060 | .060 | .060 | | | |
| $\lambda \equiv (\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | 32.79 | 32.79 | 32.79 | 32.79 | 32.79 | | | |
| Cf _o (THEOR.) × 10 ³ | .9561 | .8949 | .8415 | .8133 | .7935 | | | |
| $\zeta = \frac{2}{C_{c_0}} \lambda \qquad \text{(THEOR.)}$ | 6.858 | 7.327 | 7.792 | 8.063 | 8.264 | | | |
| δ (INCHES) | - | - | .925 | 1.175 | 1.32 | | | |
| δ* (INCHES) | - | _ | .535 | .649 | .737 | | | |
| θ (inches) | | - | .0492 | .0599 | .0660 | | | |
| H = 5*/6 | - | - | 10.87 | 10.83 | 11.17 | | | |
| n (velocity profile exponent) | - | - | 2.70 | 2.50 | 3.10 | | | |
| δ/δ _ο | | | 2.51 | 2.835 | 2.90 | | | |
| δ*/ δ ₀ * | | | 3.615 | 3.646 | 3.799 | | | |
| 6 / 6 ₀ | | | 4.134 | 4.309 | 4.429 | | | |
| н/н _о | | | .874 | .846 | .858 | | | |
| n/n _o | | | .375 | .376 | .434 | | | |
| T _w /Te _o | | | 4.04 | 3.99 | 3.94 | | | |
| P_W/P_{co} | | | 3.10 | 3.10 | 2.71 | | | |

| $M_{\infty} = 8$ $\theta_{C} = 7.25^{\circ}$ | CASE F | | | | | |
|--|--------|-----------|----------|-------|-------|--|
| N ₂ - Injectant | | AXIAL STA | TION (IN | CHES) | | |
| _ | 14.61 | 21,61 | 30.61 | 36.61 | 41.51 | |
| Re ₈ × 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 | |
| (Ou) eo FT ² SEC | | 13.21 | 13.21 | 13.21 | 13.21 | |
| (P V) LBM W FT ² SEC | | 0 | 0 | 0 | 0 | |
| $\lambda = (\rho_{\rm u} / (\rho_{\rm u})_{\rm e_{\rm o}} \times 10^4$ | | 0 | 0 | 0 | 0 | |
| Cf _o (THEOR.) × 10 ³ | | .9374 | .\$842 | .8568 | .8375 | |
| $\zeta = \frac{2}{Cf_0}\lambda$ (THEOR.) | | 0 | 0 | 0 | 0 | |
| δ _O (INCHES) | | . 208 | •357 | .393 | .458 | |
| δ ₀ * (INCHES) | | .0698 | .137 | .158 | .195 | |
| 9 ₀ (inches) | | .00593 | .0112 | .0131 | .0153 | |
| $H_0 = \delta_0^* / \theta_0$ | | 11.77 | 12.23 | 12.06 | 12.74 | |
| n (velocity profile exponent) | | 6.7 | 7.9 | 7.2 | 7.0 | |
| δ/δ ₀ | | | | | | |
| 5*/ 5,* | | | | | | |
| θ/θ_0 | | | | | | |
| н/н _о | | | | | | |
| n/n _o | | | | | | |
| T _w /Te _o | | 7.93 | 7.72 | 7.65 | 7.61 | |
| P_{w}/P_{∞} | | 2.85 | 2.86 | 2.85 | 2.86 | |

| M _a = 8 9 _c = 7.25° | CASE F $\alpha = -1^{\circ}$ (Leeward) | | | | | | |
|--|--|------------------------|-------|-------|-------|--|--|
| N2 - Injectant | | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| Res × 10 ⁻⁶ | | | | | - | | |
| (ρυ) LBM e _{o FT} ZSEC | | | | | _ | | |
| (ov) LBM W FT ⁷ SEC | | | | | 0 | | |
| $(2 (\rho v)_{\mathbf{w}} / (\rho u)_{\mathbf{e}_{0}} \times 10^{4}$ | | | | | 9 | | |
| $Cf_o(THEOR.) \times 10^3$ | | | | | | | |
| $c = \frac{2}{C_{f_0}} \lambda$ (THEOR.) | | | | | 0 | | |
| δ (INCHES) | | | | | .540 | | |
| δ* (INCHES) | | | | | .238 | | |
| θ (INCHES) | | | | | .0196 | | |
| $H = \delta^*/\theta$ | | | | | 12.12 | | |
| n (velocity profile exponent) | | , | | | 7.1 | | |
| $\delta/\delta_{\alpha=0}$ | | | | | 1.18 | | |
| $\delta^*/\delta^*_{\alpha=0}$ | | | | | 1.22 | | |
| $\theta / \theta_{\alpha=0}$ | | | | | 1.28 | | |
| H/H _{α = 0} | | | | | 0.950 | | |
| $n/n \alpha = 0$ | | | | | 1.0 | | |
| T _w /Te _o | | | | | .61 | | |
| P_{w}/P_{∞} | | | | | 2,60 | | |

| M = 8 | $\frac{\text{CASE } \underline{F} \text{(Windward)}}{\text{(Windward)}}$ | | | | | |
|--|---|-------|-------|-------|-------|--|
| $\theta_{\rm c} = 7.25^{\circ}$ | | | | | | |
| N ₂ - Injectant | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Reg x 10 ⁻⁶ | | | | | - | |
| (o u) _e LBM FT ² SEC | | | | | - | |
| (pv) LBM FT ² SEC | | | | | 0 | |
| $\lambda \equiv (\rho_{v})_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | | | | 0 | |
| Cf _o (THEOR.) × 10 ³ | | | | | - | |
| $\zeta = \frac{2}{Cf_0}\lambda$ (THEOR.) | | | | | 0 | |
| δ (INCHES) | | | | | .370 | |
| δ* (INCHES) | | | | | .162 | |
| θ (INCHES) | | | | | .0137 | |
| $H = \delta^*/\theta$ | | | | | 11.78 | |
| n (velocity profile exponent) | | | | | 7.0 | |
| $\delta / \delta_{\alpha = 0}$ | | | | | .809 | |
| $\delta^* / \delta^*_{\alpha = 0}$ | | | | | .830 | |
| $\theta / \theta_{\alpha = 0}$ | | | | | .895 | |
| $H/H_{\alpha} = 0$ | | | | | .923 | |
| $n/n \chi = 0$ | | | | | 1.0 | |
| T _w /Te _o | | | | | 7.61 | |
| Pw/Poo | | | | | 3.40 | |

| M = 8 | CASE G | | | | | | |
|---|------------------------|--------|--------|---|--------|--|--|
| $\theta_c = 7.25^{\circ}$ $N_2 - Injectant$ | AXIAL STATION (INCHES) | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| Res x 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 | | |
| (pu)e LBM FTZSEC | | 13.21 | 13.21 | 13.21 | 13.21 | | |
| (pv) LBM FT ² SEC | | .00379 | .00379 | .00379 | .00379 | | |
| $\lambda = (\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | | 2.869 | 2.869 | - 2.869 | 2.869 | | |
| Cf _o (THEOR.) × 10 ³ | | - | .8842 | ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,, | .8375 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | i | | .649 | | .685 | | |
| ð (INCHES) | | - | .400 | - | .505 | | |
| ð* (Inches) | | | .169 | - | .224 | | |
| θ (inches) | | _ | .0146 | • | .0186 | | |
| $H = \delta^*/\theta$ | | - | 12.05 | • | 12.04 | | |
| n (velocity profile exponent) | | - | 6.9 | u u | 7.3 | | |
| δ / δ _ο | | | 1.12 | | 1.105 | | |
| 8 8 8 8 | | | 1.233 | | 1.149 | | |
| 6/6, | | | 1.250 | | 1.216 | | |
| н/н _о | | | .985 | | .945 | | |
| n/n _o | | | .873 | | 1.04 | | |
| T _w /Te _O | | | 7.33 | | 7.24 | | |
| P _w /P | | | 2.83 | | 2.90 | | |

H = 8

CASE H

| 0 _c = 7.25° | | | | | |
|--|-------|-----------|----------|--------|--------|
| N ₂ - Injectant | | AXIAL STA | TION (II | NCHES) | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res × 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 |
| (pu)e LBM o FT ² SEC | | 13.21 | 13.21 | 13.21 | 13.21 |
| (pv) LBM w FT ² SEC | | .00803 | .00803 | .00803 | .00803 |
| $\lambda = (\rho v)_{\mathbf{w}} / (\rho u)_{\mathbf{e}_{\mathbf{o}}} \times 10^4$ | 4 | 6.079 | 6.079 | 6.079 | 6.079 |
| Cfo(THEOR.) x 103 | | .9374 | .8842 | .8568 | .8375 |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | 1.297 | 1.375 | 1.419 | 1.452 |
| δ (INCHES) | | .338 | .500 | .570 | .658 |
| δ* (INCHES) | | .128 | .213 | .245 | . 282 |
| θ (INCHES) | | .0118 | .0175 | .0211 | .0243 |
| n = 0*/θ | | 10.85 | 12.17 | 11.61 | 11.60 |
| n (velocity profile exponent) | | 6.4 | 7.1 | 6.2 | 6.45 |
| δ / δ _ο | | 1.425 | 1.40 | 1.45 | 1.445 |
| δ*/ δ*o | | 1.834 | 1.555 | 1.551 | 1.446 |
| θ / θ. ο | | 1.990 | 1.563 | 1.611 | 1.588 |
| и/н _о | | .922 | .945 | .963 | .910 |
| n/n _o | | .955 | .898 | .861 | .921 |
| T _w /Te _o | | 7.07 | 6.91 | 6.84 | 6.79 |
| P _w /P _{ee} | | 2.90 | 2.80 | 2.84 | 2.68 |

| н _ш = 8 6 _c = 7.25° | CASE J | | | | | | | |
|---|--------|------------------------|--------|--------|--------|--|--|--|
| N ₂ - Injectant | | AXIAL STATION (INCHES) | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | | |
| Res x 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 | | | |
| (pu) LBH o FT ² SEC | | 13.21 | 13.21 | 13.21 | 13.21 | | | |
| (pv) LBM W FT ² SEC | | .02206 | .02206 | .02206 | .02206 | | | |
| $\lambda = (\rho v)_{W} / (\rho u)_{e_{Q}} \times 10^{4}$ | | 16.70 | 16.70 | 16.79 | 16.70 | | | |
| Cf _o (THEOR.) × 10 ³ | | .9374 | .8842 | .8568 | £375 | | | |
| $\zeta = \frac{2}{Cf_Q} \lambda$ (Theor.) | | | 3.777 | | 3.988 | | | |
| δ (inches) . | | _ | .735 | • | .925 | | | |
| δ* (INCHES) | | _ | .348 | • | .476 | | | |
| θ (INCHES) | | - | .0306 | - | .0409 | | | |
| R = δ*/θ | | - | 11.35 | - | 11.64 | | | |
| n (velocity profile exponent) | | - | 5.35 | - | 4.40 | | | |
| 8/8 ₀ | | | 2.06 | | 2.02 | | | |
| 8*/ 8*0 | | | 2.54 | | 2.441 | | | |
| θ / 6. | | | 2.73 | | 2.673 | | | |
| н/н _о | | | .928 | | .914 | | | |
| n/n _o | | | .677 | | .629 | | | |
| T.,/Teo | | | 5.71 | | 5.66 | | | |
| P _w /P_ | | | | 1 | 1 | | | |

CASE M

H_a" 8 t_c = 7,25°

| $\theta_{c} = 7.25^{\circ}$ $N_{2} - Injectant$ | AXIAL STATION (INCHES) | | | | | | |
|---|------------------------|----------------|--------|---------------|--------|--|--|
| 112 2113 COC 3112 | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| Reg x 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 | | |
| (Pu)e LBM o FT ² SEC | | 13.21 | 13.21 | 13.21 | 13.21 | | |
| (PV) LBM W FT ^Z SEC | | .00422 | .00422 | .01265 | .01265 | | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | 3.195 | 3.195 | 9. 576 | 9.576 | | |
| Cf _o (THEOR.) × 10 ³ | | .9374 | .8842 | .8568 | .8375 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | .682 | •723 | 2.235 | 2.287 | | |
| å (INCHES) | | .290 | •445 | •505 | .590 | | |
| δ* (INCHES) | | .0943 | .175 | .232 | .281 | | |
| 9 (INCHES) | | .00978 | .0153 | .0199 | .0237 | | |
| $n = 5^*/\theta$ | | 9.64 | 11.44 | 11.66 | 11.36 | | |
| n (velocity profile exponent) | | 6.8 7.15 | 7.10 | 4.95 | 5.30 | | |
| δ/δο | | 1.395 | 1.245 | 1.285 | 1.29 | | |
| 8 8 8 | | 1.350 | 1.277 | 1.468 | 1.441 | | |
| θ / ÷, | | 1.650 | 1.366 | 1.519 | 1.549 | | |
| н/н _о | | .819 | .935 | .967 | .931 | | |
| n/n _o | | 1.015 1.067 | .900 | . 688 | .757 | | |
| T _w /Te _o | | 7.47 | 7.30 | 6.37 | 6.33 | | |
| P _₩ /P _∞ | | 2.80 | 2.78 | 3.20 | 2.93 | | |

| M = 8 | | | CASE | N |
|----------------------------|-------|----------|----------|-------|
| 0 _c = 7.25° | - | | | |
| N ₂ - Injectant | | AXIAL ST | ATION (1 | NCHES |
| | 14.61 | 21.61 | 30.61 | 36. |

| 8 _c = 7.25° | | | | | | |
|--|------------------------|--------|--------|-----------|--------|--|
| N2 - Injectant | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res × 10 ⁻⁶ | | 7.23 | 10.25 | 12.25 | 13.89 | |
| (pu) LBM FT ² SEC | | 13.21 | 13.21 | 13,21 | 13.21 | |
| (ρ _V) LBM W FT ² SEC | | .01158 | .01158 | .03474 | .03474 | |
| $\lambda = (\rho v)_{W} / (\rho u)_{\Theta_{O}} \times 10^{4}$ | | 8.766 | 8.766 | 26.30 | 26.30 | |
| Cfo(THEOR.) × 103 | | .9374 | .8842 | .8568 | .8375 | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | 1.983 | | 6.280 | |
| δ (INCHES) | | - | .608 | - | .925 | |
| å* (INCHES) | | - | .240 | - | .506 | |
| θ (INCHES) | | - | .0227 | - | .0398 | |
| $H = \delta^*/\theta$ | | - | 10.57 |)- | 12.71 | |
| n (velocity profile exponent) | | | 6.4 | - | 3.15 | |
| δ / δ ₀ | | | 1.705 | - | 2.02 | |
| δ*/ δ*ο | | | 1.752 | | 2.595 | |
| θ / θ, ο | | | 2.027 | | 2.601 | |
| н/но | | | .864 | | .998 | |
| n/n _o | | | .810 | | .450 | |
| T _w /Te _o | | | 6.59 | | 4.92 | |
| P _W /P _{ee} | | | 2.75 | | 3.25 | |

| H = 8 | CASE BB | | | | | | |
|--|------------------------|-------|-------|--------|-------|--|--|
| $\theta_{\rm c} = 7.25^{\circ}$ | | | | | | | |
| CO ₂ - Injectant | AXIAL STATION (INCHES) | | | | | | |
| Res x 10 ⁻⁶ | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| (pu) LBM FT ² SEC | | | | 18.3 | | | |
| (pv) LBM W FT ² SEC | | | | .00771 | | | |
| $\lambda = (\rho v)_{\mathbf{w}} / (\rho u)_{\mathbf{e}_{\mathbf{o}}} \times 10^4$ | | | | 4.213 | | | |
| Cf _o (THEOR.) × 10 ³ | | | | .8133 | | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | | 1.035 | | | |
| ð (inches) | | | | 525ء | | | |
| 8 * (INCHES) | | | | .257 | | | |
| θ (Inches) | | | | .0174 | | | |
| $H = \delta^*/\theta$ | | | | 14.76 | | | |
| n (velocity profile exponent) | | | | 6.9 | | | |
| δ/δ ₀ | | | | 1.265 | | | |
| 8*/ 8*0 | | | | 1.440 | | | |
| θ / θ, ο | | | | 1.250 | | | |
| н/н _о | | | | 1.150 | | | |
| n/n _o | | | | 1.04 | | | |
| T _w /Te _O | | | | 6.73 | | | |
| P _w /P _m | | | | 2.54 | | | |

| H = 8 | | CASE CC | | | | | |
|---|------------------------|---------|-------|--------------|-------|--|--|
| $\theta_{\rm C} = 7.25^{\rm o}$ $N_2 - Injectant$ | AXIAL STATION (INCHES) | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36,61 | 41.51 | | |
| Res × 10 ⁻⁶ | | | | 16.0 | | | |
| (pu)eo LBM FT ² SEC | | | | 18.3 | | | |
| (ρ _V) LBM W FT ² SEC | | | | .01585 | | | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | | | 8.661 | | | |
| Cf _o (THEOR.) × 10 ³ | | | | .8133 | | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | | 2.13 | | | |
| δ (INCHES) | | | | . 550 | | | |
| δ* (INCHES) | | | | .277 | | | |
| θ (INCHES) | | | | .0216 | | | |
| $H = \delta^*/\theta$ | | | | 12.81 | | | |
| n (velocity profile exponent) | | | | 5.35 | | | |
| δ / δ _ο | | | | 1.325 | | | |
| δ*/ δ*ο | | | | 1.555 | | | |
| 6 / e, 。 | | | | 1.555 | | | |
| н/н _о | | | | 1.00 | | | |
| n/n _o | | | | .805 | | | |
| T _w /Te _o | | | | 6.02 | | | |
| P _W /P _m | | | | 2.68 | | | |

| M _m = 8 θ _c = 7.25° | CASE EE | | | | | |
|---|------------------------|-------|-------|-------|-------|--|
| CO ₂ - Injectant | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res × 10 ⁻⁶ | | | | 16.0 | | |
| (pu) LBM OFT ² SEC | | | | 18.3 | | |
| (pv) LBM W FT ² SEC | | | | .0708 | | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_0} \times 10^4$ | | | | 38.67 | | |
| $Cf_o(THEOR.) \times 10^3$ | | | | .8133 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | | 9.52 | | |
| ð (INCHES) | | | | 1.150 | | |
| 8 * (INCHES) | | | | .673 | | |
| θ (INCHES) | | | | .0587 | | |
| $H = \delta^*/\theta$ | | | | 11.45 | | |
| n (velocity profile exponent) | | | | 2.35 | | |
| δ/δ ₀ | | | | 2.79 | | |
| δ*/ δ*o | | | | 3.79 | | |
| θ / θ, ο | | | | 4.22 | | |
| н/н _о | | | | .894 | | |
| n/n _o | | | | 354 | | |
| T _w /Te _o | | | | 3.85 | | |
| P_{W}/P_{oo} | | | | 3.22 | | |

| $H_{c} = 8$ $\theta_{c} = 7.25^{\circ}$ | CASE FF | | | | | |
|---|-------------------------|-------|--------|--------|-------|--|
| N ₂ - Injectant | A'(IAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res x 10 ⁻⁶ | | | 10.25 | 12.25 | 13.89 | |
| (Ou) LBM OFT ² SEC | | | 13.21 | 13.21 | 13.21 | |
| (PV) LBM W FT ² SEC | | | 0 | 0 | 0 | |
| $\lambda = (\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | | | 0 | 0 | 0 | |
| Cfo(THEOR.) × 10 ³ | | | .8842 | .8568 | .8375 | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | 0 | 0 | 0 | |
| ð (INCHES) | | | .325 | .370 | .425 | |
| δ * (INCHES) | | | .124 | .164 | .197 | |
| θ (INCHES) | | | .00689 | .00937 | .0137 | |
| $H = \delta^*/\theta$ | | | 18.02 | 17.53 | 14.35 | |
| ii (velocity profile exponent) | | | 11.2 | 8.2 | 7.9 | |
| 8/6 ₀ | | | | | | |
| 8*/ 8. | | | | | | |
| θ / θ, ο | | | X | | | |
| н/но | | | | | | |
| n/n _o | | | | | | |
| T _w /Te _o | | | 7.65 | 7.60 | 7.63 | |

Pw/P

2,82

2.84

2.77

| н <u> </u> = 8 | | | CASE | GG | • |
|---|-------|----------|----------|---------------|--------|
| $\theta_{\rm c} = 7.25^{\rm o}$ | | | | | |
| N ₂ - Injectant | | AXIAL ST | ATION (I | NCHES) | |
| _ | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res x 10 ⁻⁶ | | | | 11.98 | 13.58 |
| (pu) LBM FT ² SEC | | | | 12.92 | 12.92 |
| (pv) LBM FT ² SEC | | | | .00614 | .00595 |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_0} \times 10^4$ | | | | 4,752 | 0 |
| Cfo(THEOR.) x 103 | | | | .8 568 | .8375 |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | | 1.110 | 0 |
| δ (INCHES) | | | | .510 | •550 |
| δ [*] (INCHES) | | | | - | .133 |
| θ (INCHES) | | | | - | .0120 |
| $H = \delta^*/\theta$ | | | | - | 11.07 |
| n (velocity profile exponent) | | | | • | 6.8 |
| δ/δ ₀ | | | | - | 1.200 |
| δ*/ δ*· | | | | | |
| θ / e _{. o} | | | | | |
| н/н _о | | | | | |
| n/n _o | | | | | |
| T _w /Te _o | | | | 7.08 | 7.03 |
| P _w /P _m | | | | 2.71 | 2.61 |

| Η_= 8 θ _C = 7.25° | CASE KK | | | | |
|---|---------|----------|----------|--------|-------|
| N ₂ - Injectant | | AXIAL ST | ATION (I | NCHES) | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res × 10 ⁻⁶ | | | | 12.25 | |
| (Pu)eo LBM | | | | 13.21 | |
| (pv) LBM W FT ² SFC | | | | .0519 | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | | | 39.29 | |
| $Cf_{o}(THEOR.) \times 10^{3}$ | | | | .8568 | |
| $\zeta = \frac{2}{Cf_Q} \lambda$ (THEOR.) | | | | 9.18 | |
| ð (Inches) | | | | 1.10 | |
| 6 * (INCHES) | | | | .624 | |
| 0 (Inches) | | | | .0638 | |
| $H = \delta^*/\theta$ | | | | 9.781 | - |
| n (velocity profile exponent) | | | | 2.05 | |
| δ/δ ₀ | | | | 2.80 | |
| δ*/ δ*· | | | | 3.95 | |
| θ / θ. ο | | | | 4.87 | |
| н/н _о | | | | .811 | |
| n/n _o | | | | . 285 | |
| T _w /T _{e₀} | | | | 4.45 | |
| P _w /P _w | | | | 3.20 | |

| н 8 | CASE PL | | | | | |
|---|------------------------|-------|--------------|--------------|-------|--|
| θ _c = 7.25° | | | | | | |
| N2 - Injectant | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res x 10 ⁻⁶ | | | 1.684 | 2.645 | | |
| (Pu) LBM OFT ² SEC | | | 5.24 | 6.07 | | |
| (PV) LBM W FT ² SEC | | | 0 | 0 | | |
| $\lambda = (\rho v)_{\text{W}} / (\rho u)_{\text{e}_{0}} \times 10^{4}$ | | | 0 | 0 | | |
| Cf _o (THEOR.) × 10 ³ | | | .8 31 | . 664 | | |
| $\frac{2}{C_{f_0}}\lambda$ (THEOR.) | | | 0 | 0 | | |
| 6 (INCHES) | | | .125 | .150 | | |
| δ [*] (INCHES) | | | ,0789 | .0199 | | |
| θ (INCHES) | | | .0119 | .00254 | | |
| $H = \delta^*/\theta$ | | | 6.611 | 7.827 | ÷ | |
| n (velocity profile exponent) | | | _ | | | |
| δ / δ ₀ | | | | | | |
| δ*/ δ*· | | | | | | |
| 6 / 6, o | | | X | | | |
| и/н _о | | | | | | |
| n/n _o | | | | | | |
| T _u /Te _o | | | 9.39 | 8.88 | | |
| Pu/Pe | | | 2.62 | 2.68 | | |

2.62 2.68

| и_ = 8 6 _c = 7.25° | CASE QL | | | | |
|--|---------|----------|----------|--------|-------|
| N ₂ - Injectant | | AXIAL ST | ATION (I | NCHES) | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res × 10 ⁻⁶ | | | | 2.645 | |
| (pu)e LBMO FT ² SEC | | | | 6.07 | |
| (ρ _V) LBM FT ² SEC | | | | .0584 | |
| $\lambda \equiv (\rho v)_{W} / (\rho u)_{e_{0}} \times 10^{4}$ | | | | 96.2 | |
| $Cf_o(THEOR.) \times 10^3$ | | | | .664 | |
| $\zeta = \frac{2}{Cf_O} \lambda$ (THEOR.) | | | | 28.98 | |
| ð (Inches) | | | | 1.250 | |
| δ* (INCHES) | | | | .893 | |
| θ (INCHES) | | | | .0512 | |
| H = δ*/θ | | | | 17.45 | |
| n (velocity profile exponent) | | | | - | |
| δ / δ _σ | | | | 8.34 | |
| δ*/ δ*ο | | | | 44.0 | |
| θ / θ _{. o} | | | | 19.7 | |
| н/н _о | | | | 2.235 | |
| n/n _o | | | | • | |
| T _u / _{Teo} | | | | 5.51 | |
| P _w /P _w | | | | 3.20 | |

| M - | 8 |
|------------------|-------|
| θ _c - | 7.25° |

CASE RL

| N ₂ - | Injectant |
|------------------|-----------|
| | |

| N ₂ - Injectant | AXIAL STATION (INCHES) | | | | |
|--|------------------------|-------|--------|-------|-------|
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Re ₈ x 10 ⁻⁶ | | | .576 | .798 | |
| (pu)e LBM FT ² SEC | | | 2.835 | 3.093 | |
| (PV) LBM W FT ² SEC | | | 0 | 0 | |
| $\lambda \equiv (\rho v)_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | | 0 | 0 | |
| Cf _o (THEOR.) × 10 ³ | | | 1.318 | 1.169 | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | 0 | ٥ | |
| δ (INCHES) | | | .125 | .150 | |
| δ* (INCHES) | | | .0580 | .0821 | |
| θ (INCHES) | | | .00966 | .0125 | |
| $H = \delta^*/\theta$ | | | 6.01 | 6.55 | |
| n (velocity profile exponent) | | | _ | | |
| δ/δο | | | | | |
| δ*/ δ*ο | | | | | |
| θ / θ. | | | X | | |
| H/H ₀ | | | | | |
| n/n _o | | | | | |
| T _u /Te _o | | | 7.86 | 7.65 | |
| P _w /P _m | | | 2.22 | 2.32 | |

| H_ = 8 | CASE SL | | | | | |
|---|------------------------|-------|-------|-------|----------|--|
| θ _c = 7.25° | | | | | | |
| N2 - Injectant | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res × 10 ⁻⁶ | | | | .798 | | |
| (pu) LBM FT ² SEC | | | | 3.093 | | |
| (pv) LBM FT ² SEC | | | | .0573 | Í | |
| $(\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | | | | 185.3 | | |
| Cf _o (THEOR.) × 10 ³ | | | | 1.169 | | |
| $\frac{2}{Cf_Q}\lambda$ (THEOR.) | | | | 31.7 | | |
| 6 (INCHES) | | | | 1.550 | | |
| 6 * (INCHES) | | | | 1.028 | | |
| θ (INCHES) | | | | .0991 | | |
| H = δ*/θ | | | ļ | 10.37 | <u> </u> | |
| n (velocity profile exponent) | | | | - | | |
| 8 / 8 ₀ | | | | 10.33 | | |
| δ*/ δ*ο | | | | 12.52 | | |
| θ / θ _{. o} | | | | 7.93 | | |
| н/н _о | | | | 1.58 | | |
| n/n _o | | | | | | |
| T _w /Te _o | | | | 5.51 | | |
| Pw/P | | | | 2 9/ | | |

CASE TL

 $M_{c} = 8$ $\theta_{c} = 7.25^{\circ}$

| N_2 - Injectant | AXIAL STATION (INCHES) | | | | |
|--|------------------------|-------|--------|--------------|-------|
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res x 10 ⁻⁶ | | | 2.619 | 3.217 | 3.55 |
| (Qu)eo LBM FT ² SEC | | | 3.056 | 3.056 | 3.056 |
| (ρ _V) LBM W FT ² SEC | | | .00116 | .00118 | 0 |
| $\lambda \equiv (\rho v)_{\rm w} / (\rho u)_{\rm e_0} \times 10^4$ | | | 3.796 | 3.861 | C |
| Cf _o (THEOR.) × 10 ³ | | | .711 | . 650 | .610 |
| C_{f_0} (THEOR.) | | | 1.068 | 1.188 | 0 |
| δ (11.3) | | | .375 | .430 | .488 |
| δ * (INCHES) | | | .249 | .259 | .210 |
| 6 (INCHES) | | | .0141 | .0180 | .0221 |
| $H = \delta^*/\theta$ | | | 17.63 | 14.40 | 9.46 |
| n (velocity profile exponent) | | | _ | - | • |
| δ/δ _ο | | | 1.62 | 1.70 | 1.82 |
| δ*/ δ*o | | | 1.28 | 1.22 | .928 |
| θ / θ, ο | | | 1.94 | 2.27 | 2.62 |
| н/но | | | .657 | .537 | .353 |
| n/n _o | | | | - | - |
| T _w /Te _o | | | 7.14 | 7.65 | 7.14 |
| Pw/P,, | | | 2.ú8 | 2,58 | 2.51 |

M_ - 8

CASE UL

| θ _C = | 7.25° |
|------------------|-------|
|------------------|-------|

| $\theta_{\rm c} = 7.25^{\circ}$ $N_2 = Injectant$ | | AXIAL ST | ATION (I | CHES) |] |
|---|-------|----------|----------|--------|-------|
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 |
| Res x 10 ⁻⁶ | ^} | | 2.619 | 3.217 | 3.55 |
| (nu) eo LBM | | | 3.056 | 3.056 | 3.056 |
| (pv) LBM W FT ² SEC | | | .00245 | .00264 | 0 |
| $\lambda = (\rho v)_{W} / (\rho u)_{x} \times 10^{4}$ | | | 8.017 | 8.639 | 0 |
| Cfo(THEOR.) × 10 ³ | | | .711 | .650 | .610 |
| $\zeta = \frac{2}{Cf_0} \lambda$ (Theor.) | | | 2.255 | 2.658 | 0 |
| ð (INCHES) | | | .460 | •500 | .525 |
| δ* (INCHES) | | | .371 | .342 | .264 |
| θ (INCHES) | | | .0141 | .0198 | .0198 |
| $H = \delta^*/\theta$ | | | 26.41 | 17.27 | 13.35 |
| n (velocity profile exponent) | | | - | - | - |
| 8 / 8 ₀ | | | 1.99 | 1.98 | 1.95 |
| 5*/ 5*0 | | | 1.90 | 1.61 | 1.17 |
| θ / θ, ο | | | 1.94 | 2.50 | 2.35 |
| н/н _о | | | .984 | .644 | .498 |
| n/n _o | | | • | - | - |
| T _w /Te _o | | | 5.20 | 7.35 | 7.14 |
| P_{w}/P_{w} | | | 2.91 | 2.77 | 2.53 |

| Η _ω = 8 θ _C = 7.25° | CASE VL | | | | | |
|--|---------|----------|----------|-------|-------|--|
| N ₂ - Injectant | | AXIAL ST | ATION (I | CHES) | | |
| - | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res × 10 ⁻⁶ | | | .842 | 1.277 | | |
| (Ou)e LBM FT ² SEC | | | 1.668 | 1,952 | | |
| (pv) LBM W FT ² SEC | | | 0 | 0 | | |
| $\lambda \equiv (\rho v)_{w} / (\rho u)_{e_{o}} \times 10^{4}$ | | | 0 | 0 | | |
| Cf _o (THEOR.) x 10 ³ | | | 1.221 | .994 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | 0 | 0 | | |
| δ (INCHES) | | | .225 | . 250 | | |
| 8 * (INCHES) | | | .150 | .172 | | |
| θ (INCHES) | | | .0183 | .0163 | | |
| $H = \delta^*/\theta$ | | | 8.20 | 10.59 | | |
| n (velocity profile exponent) | | | • | • | | |
| δ / δ ₀ | | | | | | |
| δ*/ δ*o | | | | | | |
| θ / θ, ο | | | > | | | |
| н/н _о | | | | | | |
| n/n _o | | | | | | |
| T _w /Te _o | | | 6.94 | ó.94 | | |
| P_{w}/P_{∞} | | | 2.80 | 2.59 | | |

| Η _ω = 8 θ _C = 7.25° | CASE WL AXIAL STATION (INCHES) | | | | | |
|---|---------------------------------|-------|--------|--------|-------|--|
| N ₂ - Injectant | | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Res x 10 ⁻⁶ | | | .842 | 1.277 | | |
| (Pu) eo FT ² SEC | | | 1.668 | 1.952 | | |
| (ρ _V) LBM W FT ² SEC | | | .00112 | .00116 | | |
| $\lambda = (\rho v)_{w} / (\rho u)_{e_o} \times 10^4$ | | | 6.715 | 5.943 | | |
| Cf _o (THEOR.) × 10 ³ | | | 1.221 | .994 | | |
| $\frac{2}{cf_0}\lambda$ (THEOR.) | | | 1.100 | 1.196 | | |
| δ (INCHES) | | | .425 | .450 | | |
| ô* (INCHES) | | | . 295 | .301 | | |
| θ (INCHES) | | | .0163 | .0124 | | |
| $H = \delta^*/\theta$ | | | 18.04 | 24.22 | | |
| n (velocity profile exponent) | | | - | - | | |
| δ/δ ₀ | | | 1.89 | 1.80 | | |
| δ*/ δ*ο | | | 1.97 | 1.75 | | |
| 9 / e. | | | .891 | .761 | | |
| н/н _о | | | 2.20 | 2.29 | | |
| n/n _o | | | - | - | | |

 T_w/T_{e_o}

P_W/P_{co}

6.22

2.48

6.22

2.44

| ж° = 8 | | | CASE | XI. | | |
|--|------------------------|-------|--------------|--------|---------------------------------------|--|
| $\theta_{\rm c} = 7.25^{\rm o}$ | | | | | | |
| N ₂ - Injectant | AXIAL STATION (INCHES) | | | | | |
| | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | |
| Re ₈ x 10 ⁻⁶ | • | | .842 | 1.277 | | |
| (Pu)e EBM | | | 1.668 | 1.952 | | |
| (ρ _V) LBM W FT ² SEC | | | .00263 | .00210 | | |
| $\lambda \equiv (\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | | | 15.77 | 10.76 | · · · · · · · · · · · · · · · · · · · | |
| Cf _O (THEOR.) x 10 ³ | | | 1.221 | •994 | | |
| $\frac{2}{Cf_0}\lambda$ (THEOR.) | | | 2.583 | 2.165 | | |
| δ (INCHES) | | | . 575 | .600 | | |
| δ* (INCHES) | | | .455 | .476 | | |
| θ (INCHES) | | | .0342 | •0336 | | |
| н = 8*/8 | | | 13.31 | 14.15 | | |
| n (velocity profile exponent) | | | - | ٠. | | |
| δ/δο | | | 2.56 | 2.40 | | |
| 5 / 5 0 | | | 3.03 | 2.77 | | |
| θ/θ. | | | 1.87 | 2.06 | | |
| н/н _о | | | 1.62 | 1.34 | | |
| n/n _o | | | ~ | - | | |
| T _w /Te _o | | | 5.10 | 4.90 | | |
| P _w /P _{ee} | | | 2.81 | 2.48 | | |

| M_ = 8 | m = 0 Case Corresponding to UL, TL (VIZAAD) | | | | | | |
|--|---|-------|--------|--------|--------|--|--|
| $\theta_c = 7.25^{\circ}$ | | | | | | | |
| N ₂ - Injectant | AXIAL STATION (INCHES) | | | | | | |
| 6 | 14.61 | 21.61 | 30.61 | 36.61 | 41.51 | | |
| Res x 10 ⁻⁶ | | | 2.66 | 3.16 | 3.60 | | |
| (Ou) LBM FT ² SEC | | | 3.115 | 3.105 | 3.105 | | |
| (ρ _V) LBM W FT ² SEC | | | 0 | 0 | 0 | | |
| $\lambda \equiv (\rho v)_{W} / (\rho u)_{e_{O}} \times 10^{4}$ | | | 0 | 0 | 0 | | |
| Cf _o (THEOR.) × 10 ³ | | | .701 | .644 | .604 | | |
| $\zeta = \frac{2}{Cf_0} \lambda$ (THEOR.) | | | 0 | 0 | 0 | | |
| ð (INCHES) | | | .231 | . 252 | . 269 | | |
| δ* (INCHES) | | | .195 | .212 | . 226 | | |
| θ (Inches) | | | .00726 | .00792 | .00844 | | |
| $H = \delta^*/\theta$ | | | 26.84 | 26.83 | 26.82 | | |
| n (velocity profile exponent) | | | - | - | - | | |
| 6/6 ₀ | | | | | | | |
| δ*/ δ*ο | | | | | | | |
| θ / θ, ο | | | | | | | |
| н/н _о | | | | | | | |
| n/n _o | | | | | | | |
| T _w /Te _o | | | 7.28 | 7.28 | 7.28 | | |
| P _W /P _m | | | | | | | |